

# Flavor gauge models below the Fermi scale

1705.01822

Pedro A. N. Machado  
Fermilab

*in collaboration with Kaladi Babu, Alex Friedland and Irina Mocioiu*



Can there be flavor mediators at a low scale???

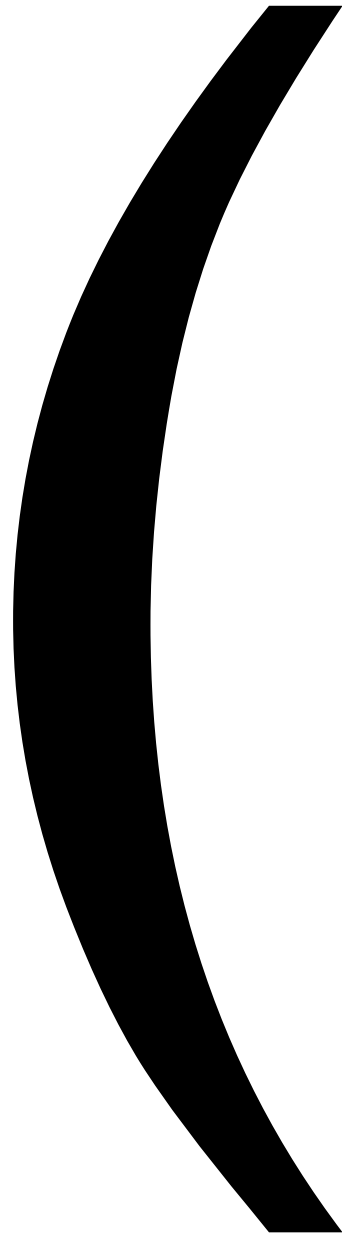
Flavor physics is definitely heavy

With minimal flavor violation: above TeV scale

Without minimal flavor violation: above 1000 TeV scale

see e.g. D'Ambrosio, Giudice, Isidori, Strumia 2002

Is it?



## Studies for $(B^+)L_\mu-L_\tau$ at low energies

Heeck Rodejohann 2011, Altmannshofer et al 2014, Altmannshofer et al 2015, Farzan 2015, Farzan Shoemaker 2015, Heck 2016, Altmannshofer et al 2016, Forero Huang 2016, ...

Motivation:

$(g-2)_\mu$ , proton radius, large neutrino matter effects (NSI),  $h$  to  $\tau \mu$

**Non Standard Interactions:**

$$2\sqrt{2}G_F\varepsilon_{\alpha\alpha}^f (\bar{\nu}_{\alpha L}\gamma_\mu\nu_{\alpha L}) (\bar{f}\gamma^\mu f)$$

**No SU(2) invariance**

Usual lore: restoring SU(2) mostly rule out  
NSIs observable at neutrino experiments



## Studies for $(B^+)L_\mu-L_\tau$ at low energies

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Motivation:

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**Non Standard Interactions:**

$$(\bar{L}\gamma_\mu L)(\bar{Q}_L\gamma^\mu Q_L) = (\bar{\nu}_L\gamma_\mu\nu_L)(\bar{Q}_L\gamma^\mu Q_L) + (\bar{\ell}_L\gamma_\mu\ell_L)(\bar{Q}_L\gamma^\mu Q_L)$$

Charged leptons will generically provide a much stronger bound

#	Dim. eight operator	$\mathcal{C}_{LLH}^{111}$	$\mathcal{C}_{LLH}^{331}$	$\mathcal{C}_{LLH}^{133}$	$\mathcal{C}_{LLH}^{313}$	$\mathcal{C}_{LLH}^{333}$	$\mathcal{O}_{\text{NSI}}?$	Mediators
<b>Combination <math>(\bar{L}^\beta L_\alpha)(\bar{L}^\delta L_\gamma)(H^\dagger H)</math></b>								
31	$(\bar{L}\gamma^\rho L)(\bar{L}\gamma_\rho L)(H^\dagger H)$	1						$\mathbf{1}_0^v$
32	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}\gamma_\rho \bar{\tau} L)(H^\dagger H)$		1					$\mathbf{3}_0^v$
33	$(\bar{L}\gamma^\rho L)(\bar{L}\gamma_\rho \bar{\tau} L)(H^\dagger \bar{\tau} H)$			1				$\mathbf{1}_0^v + \mathbf{3}_0^v$
34	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}\gamma_\rho L)(H^\dagger \bar{\tau} H)$				1			$\mathbf{1}_0^v + \mathbf{3}_0^v$
35	$(-i\epsilon^{abc})(\bar{L}\gamma^\rho \tau^a L) \times$ $(\bar{L}\gamma_\rho \tau^b L)(H^\dagger \tau^c H)$					1	✓	$\mathbf{3}_0^v$
<b>Combination <math>(\bar{L}^\beta L_\alpha)(\bar{L}^\delta H)(H^\dagger L_\gamma)</math></b>								
36	$(\bar{L}\gamma^\rho L)(\bar{L}H)(\gamma_\rho)(H^\dagger L)$	1/2		1/2			✓	$\mathbf{1}_0^v + \mathbf{1}_0^R$
37	$(\bar{L}\gamma^\rho L)(\bar{L}\bar{\tau}H)(\gamma_\rho)(H^\dagger \bar{\tau} L)$	3/2		-1/2				$\mathbf{1}_0^v + \mathbf{3}_0^{L/R}$
38	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}\bar{\tau}H)(\gamma_\rho)(H^\dagger L)$		1/2		1/2	1/2	✓	$\mathbf{1}_0^v + \mathbf{1}_0^R + \mathbf{3}_0^{L/R}$
39	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}H)(\gamma_\rho)(H^\dagger \bar{\tau} L)$		1/2		1/2	-1/2	✓	$\mathbf{1}_0^v + \mathbf{1}_0^R + \mathbf{3}_0^{L/R}$
40	$(-i\epsilon^{abc})(\bar{L}\gamma^\rho \tau^a L) \times$ $(\bar{L}\tau^b H)(\gamma_\rho)(H^\dagger \tau^c L)$		1		-1			$\mathbf{3}_0^v + \mathbf{1}_0^R + \mathbf{3}_0^{L/R}$
<b>Combination <math>(\bar{L}^\beta L_\alpha)(\bar{L}^\delta H^\dagger)(L_\gamma H)</math></b>								
41	$(\bar{L}\gamma^\rho L)(\bar{L}i\tau^2 H^*)(\gamma_\rho)(H^T i\tau^2 L)$	-1/2		1/2				$\mathbf{1}_0^v + \mathbf{1}_{-1}^{L/R}$
42	$(\bar{L}\gamma^\rho L)(\bar{L}\bar{\tau}i\tau^2 H^*)(\gamma_\rho)(H^T i\tau^2 \bar{\tau} L)$	-3/2		-1/2				$\mathbf{1}_0^v + \mathbf{3}_{-1}^{L/R}$
43	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}\bar{\tau}i\tau^2 H^*)(\gamma_\rho)(H^T i\tau^2 L)$		-1/2		1/2	1/2		$\mathbf{3}_0^v + \mathbf{1}_{-1}^{L/R} + \mathbf{3}_{-1}^{L/R}$
44	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}i\tau^2 H^*)(\gamma_\rho)(H^T i\tau^2 \bar{\tau} L)$		-1/2		1/2	-1/2		$\mathbf{3}_0^v + \mathbf{1}_{-1}^{L/R} + \mathbf{3}_{-1}^{L/R}$
45	$(-i\epsilon^{abc})(\bar{L}\gamma^\rho \tau^a L) \times$ $(\bar{L}\tau^b i\tau^2 H^*)(\gamma_\rho)(H^T i\tau^2 \tau^c L)$		-1		-1		✓	$\mathbf{3}_0^v + \mathbf{3}_{-1}^{L/R}$
<b>Combination <math>(\bar{L}^\beta (L^c)^\delta)((\bar{L}^c)_\alpha L_\gamma)(H^\dagger H)</math></b>								
46	$(\bar{L}i\tau^2 L^c)(\bar{L}^c i\tau^2 L)(H^\dagger H)$	1/4	-1/4				✓	$\mathbf{1}_{-1}^s$
47	$(\bar{L}\bar{\tau}i\tau^2 L^c)(\bar{L}^c i\tau^2 \bar{\tau} L)(H^\dagger H)$	-3/4	-1/4					$\mathbf{3}_{-1}^s$
48	$(\bar{L}i\tau^2 L^c)(\bar{L}^c i\tau^2 \bar{\tau} L)(H^\dagger \bar{\tau} H)$			1/4	-1/4	-1/4	✓	$\mathbf{1}_{-1}^s + \mathbf{3}_{-1}^s$
49	$(\bar{L}\bar{\tau}i\tau^2 L^c)(\bar{L}^c i\tau^2 L)(H^\dagger \bar{\tau} H)$			-1/4	1/4	-1/4	✓	$\mathbf{1}_{-1}^s + \mathbf{3}_{-1}^s$
50	$(-i\epsilon^{abc})(\bar{L}\tau^a i\tau^2 L^c) \times$ $(\bar{L}^c i\tau^2 \tau^b L)(H^\dagger \tau^c H)$			-1/2	-1/2			$\mathbf{3}_{-1}^s$
<b>Combination <math>(\bar{L}^\beta H^\dagger)((L^c)^\delta H)((\bar{L}^c)_\alpha L_\gamma)</math></b>								
51	$(\bar{L}i\tau^2 H^*)(H^T L^c)(\bar{L}^c i\tau^2 L)$	1/8	-1/8	1/8	-1/8	1/8	✓	$\mathbf{1}_{-1}^s + \mathbf{1}_0^L + \mathbf{1}_{-1}^{L/R}$
52	$(\bar{L}\bar{\tau}i\tau^2 H^*)(H^T L^c \bar{\tau})(\bar{L}^c i\tau^2 L)$	-3/8	3/8	1/8	-1/8	1/8	✓	$\mathbf{1}_{-1}^s + \mathbf{3}_0^{L/R} + \mathbf{1}_{-1}^{L/R}$
53	$(\bar{L}\bar{\tau}i\tau^2 H^*)(H^T L^c)(\bar{L}^c i\tau^2 \bar{\tau} L)$	-3/8	-1/8	-3/8	-1/8	1/8	✓	$\mathbf{3}_{-1}^s + \mathbf{1}_0^L + \mathbf{3}_{-1}^{L/R}$
54	$(\bar{L}i\tau^2 H^*)(H^T \bar{\tau} L^c)(\bar{L}^c i\tau^2 \bar{\tau} L)$	3/8	1/8	-1/8	-3/8	-1/8		$\mathbf{3}_{-1}^s + \mathbf{3}_0^{L/R} + \mathbf{1}_{-1}^{L/R}$
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57	$(\bar{L}\bar{\tau}i\tau^2 L^c)(\bar{L}^c \bar{\tau} H^*)(H^T i\tau^2 L)$	3/8	1/8	-3/8	-1/8	-1/8		$\mathbf{3}_{-1}^s + \mathbf{3}_0^{L/R} + \mathbf{1}_{-1}^{L/R}$
58	$(\bar{L}i\tau^2 L^c)(\bar{L}^c \bar{\tau} H^*)(H^T i\tau^2 \bar{\tau} L)$	-3/8	3/8	-1/8	1/8	1/8	✓	$\mathbf{1}_{-1}^s + \mathbf{3}_0^{L/R} + \mathbf{3}_{-1}^{L/R}$
59	$(\bar{L}\bar{\tau}i\tau^2 L^c)(\bar{L}^c H^*)(H^T i\tau^2 \bar{\tau} L)$	-3/8	-1/8	-1/8	-3/8	1/8	✓	$\mathbf{3}_{-1}^s + \mathbf{1}_0^L + \mathbf{3}_{-1}^{L/R}$
60	$(-i\epsilon^{abc})(\bar{L}\tau^a i\tau^2 L^c) \times$ $(\bar{L}^c \tau^b H^*)(H^T i\tau^2 \tau^c L)$	3/4	1/4	1/4	-1/4	1/4		$\mathbf{3}_{-1}^s + \mathbf{3}_0^{L/R} + \mathbf{3}_{-1}^{L/R}$

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39	$(\bar{L}\gamma^\rho \bar{\tau} L)(\bar{L}\bar{\tau}H)(\gamma_\rho)(H^\dagger \bar{\tau} L)$		1/2		1/2	1/2	✓	$\mathbf{1}_0^v + \mathbf{1}_0^R + \mathbf{3}_0^{L/R}$

the neutrino sector. Since any model of new physics has to recover the Standard Model at low energies, we have required gauge invariance under the SM gauge group and studied the possible effective theories. The focus is set on purely leptonic NSI, that is, on operators in

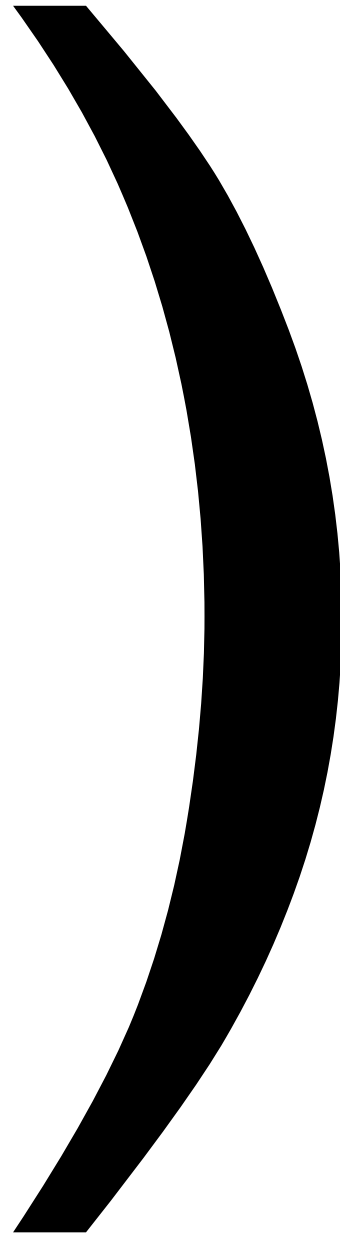
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In conclusion, we have demonstrated that the minimum complexity of a realistic model leading to large NSI and no charged lepton flavor violation requires at least two new fields inducing  $d = 8$  NSI couplings. We have determined the possible SM charges of those medi-

53	$(\bar{L}\bar{\tau}i\tau^2 H^*)(H^T L^c)(\bar{L}^c i\tau^2 \bar{\tau} L)$	-3/8	-1/8	-3/8	-1/8	1/8	✓	$\mathbf{3}_{-1}^s + \mathbf{1}_0^L + \mathbf{3}_{-1}^{L/R}$
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Gavela et al 2008





# Flavor Physics

In the SM each family provides a  
**complete independent consistent realization of the model**  
(Anomalies cancel within each family)

Why such small mixing to third family quarks?

Maybe the third family is indeed special  
and has its own gauge symmetry?

We will gauge  $B - L$  of the **third family**

$U(1)_{B-L}^{(3)}$  (let us refer to it as  $X$ )

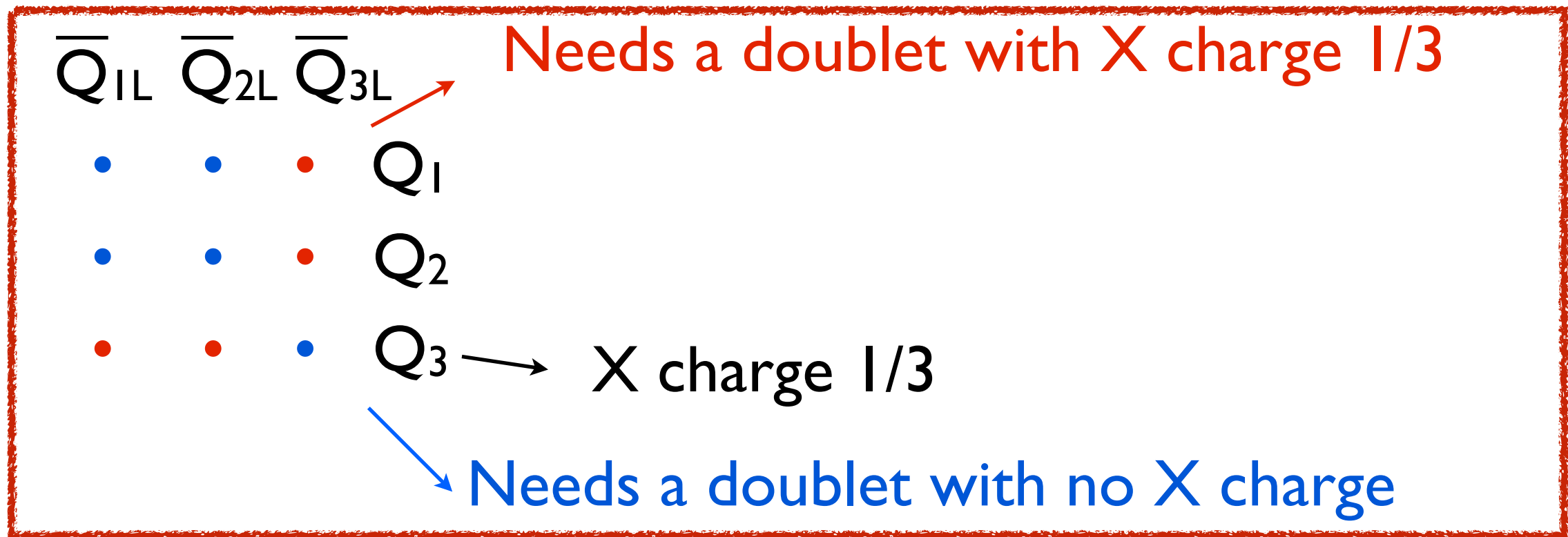
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# Flavor Physics

$u, d, c, s$	$0$
$b, t$	$+1/3$
$e, \mu, \nu_e, \nu_\mu$	$0$
$\tau, \nu_\tau$	$-1$

# Flavor Physics

u, d, c, s	0
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CKM  $\rightarrow$  extra doublet.  
 The flavor symmetry is broken by a Higgs doublet:  
 Its “natural” scale is EW

	$\phi_1$	$\phi_2$	s
$SU(2)_L$	<b>2</b>	<b>2</b>	<b>1</b>
$U(1)_Y$	+1	+1	0
$U(1)_{B-L}^{(3)}$	+1/3	0	+1/3

generating CKM

$$\overline{\mathbf{Q}}_L \begin{pmatrix} y_{11}^u \tilde{\phi}_2 & y_{12}^u \tilde{\phi}_2 & y_{13}^u \tilde{\phi}_1 \\ y_{21}^u \tilde{\phi}_2 & y_{22}^u \tilde{\phi}_2 & y_{23}^u \tilde{\phi}_1 \\ 0 & 0 & y_{33}^u \tilde{\phi}_2 \end{pmatrix} \mathbf{u}_R$$



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$$\begin{pmatrix} m_u^0 & 0 & V_{ub}^0 m_t^0 \\ 0 & m_c^0 & V_{cb}^0 m_t^0 \\ 0 & 0 & m_t^0 \end{pmatrix} \begin{pmatrix} m_d^0 & 0 & 0 \\ 0 & m_s^0 & 0 \\ am_b^0 & bm_b^0 & m_b^0 \end{pmatrix}$$

Generates flavor changing interactions in the quark sector

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$\Phi_1$  induces mass mixing between X and Z gauge bosons

$$Z_\mu \simeq -s_w B_\mu + c_w W_\mu^3 - s_X X_\mu^0, \quad M_X^2 = \frac{1}{9} g_X^2 \left( \frac{v_1^2 v_2^2}{v^2} + v_s^2 \right)$$

$$X_\mu \simeq s_X (-s_w B_\mu + c_w W_\mu^3) + X_\mu^0, \quad s_X \equiv \frac{2}{3} \frac{g_X}{\sqrt{g^2 + g'^2}} \frac{v_1^2}{v^2}$$

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$$M_X^2 = \frac{1}{9} g_X^2 \left( \frac{v_1^2 v_2^2}{v^2} + v_s^2 \right)$$

$$s_X \equiv \frac{2}{3} \frac{g_X}{\sqrt{g^2 + g'^2}} \frac{v_1^2}{v^2}$$

EWPT suggests small mixing, and thus small masses...

$$\mathcal{L}_{yuk}^{\ell} = y_{ij}^{\ell} \bar{L}_i \phi_2 \ell_{Rj}$$

No flavor changing interactions in the lepton sector

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Neutrino masses via effective operators

$$\frac{1}{\Lambda} \left( \bar{L}_{1,2} \tilde{\phi}_2 \right) \left( \phi_2^\dagger \tilde{L}_{1,2} \right), \quad \frac{1}{\Lambda^2} \left( \bar{L}_3 \tilde{\phi}_1 \right) \left( \phi_1^\dagger \tilde{L}_{1,2} \right) s^*$$

$$\text{U(1):} \quad \begin{array}{cccc} 0 & 0 & 0 & 0 \end{array} \quad \begin{array}{ccccc} -1 & +1/3 & +1/3 & 0 & +1/3 \end{array}$$

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$\theta_{12}$ : D=5

$\theta_{13}$  and  $\theta_{23}$ : D=6

No flavor changing interactions in the lepton sector!

$\Lambda$  not far from electroweak scale!

**Usual comments at this point:**

**This is ruled out**

**It is ok if one makes the gauge coupling tiny (cheating...)**

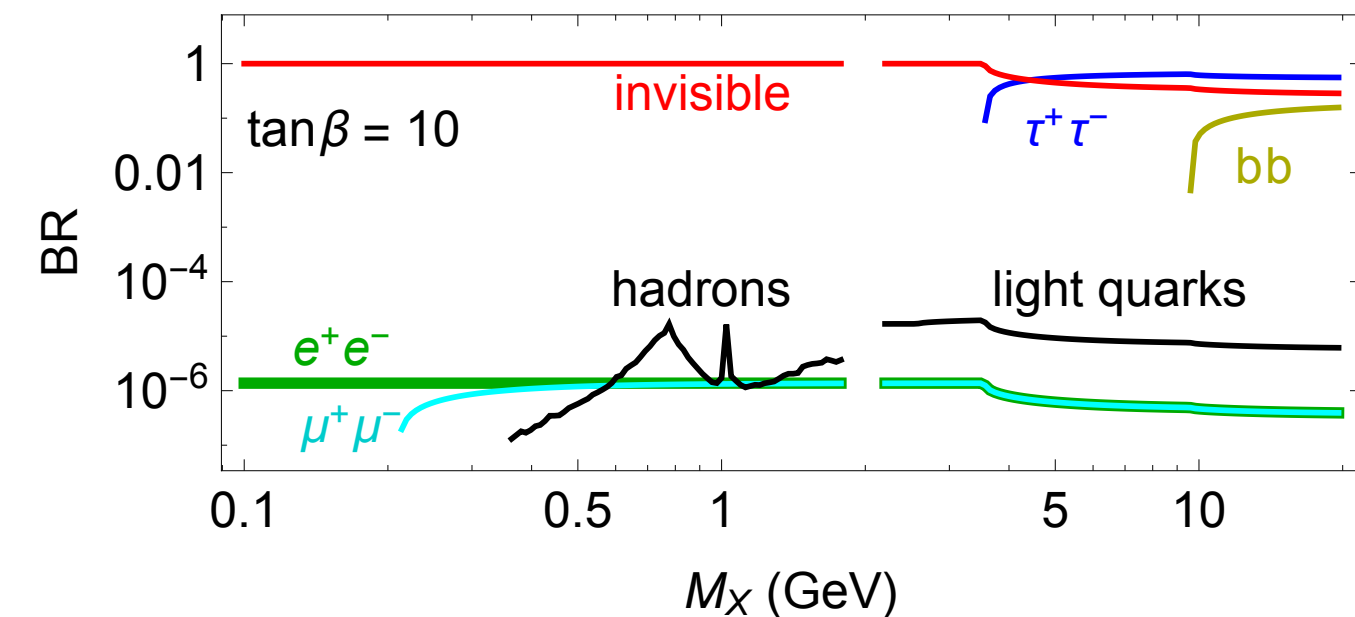
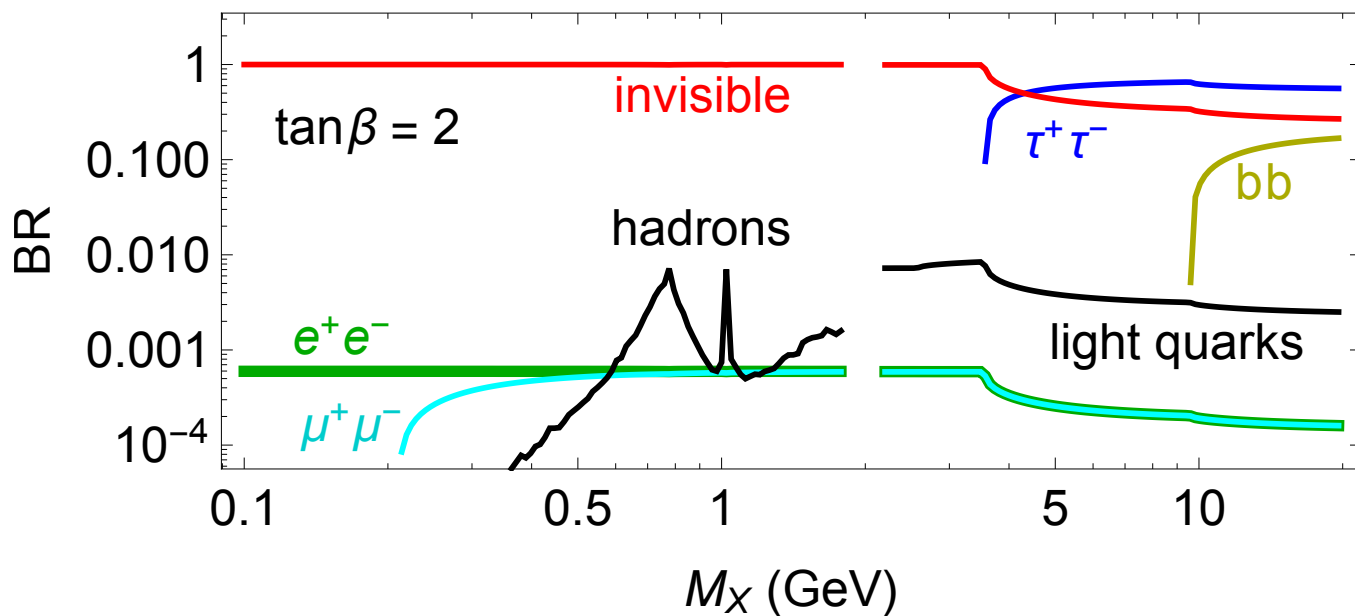


**Usual comments at this point:**

**This is ruled out** 

**It is ok if one makes the gauge coupling tiny (cheating...)** 

# Flavor Physics



$$c_\alpha = q_\alpha c_w e \varepsilon + \left( g_X q_\alpha^X + s_X \sqrt{g^2 + g'^2} q_\alpha^Z \right)$$

$$q_\alpha^Z = I_3^\alpha - s_w^2 q_\alpha$$

$$s_X \equiv \frac{2}{3} \frac{g_X}{\sqrt{g^2 + g'^2}} \frac{v_1^2}{v^2}$$

Light  $X$ :  $v_\tau v_\tau$  dominates

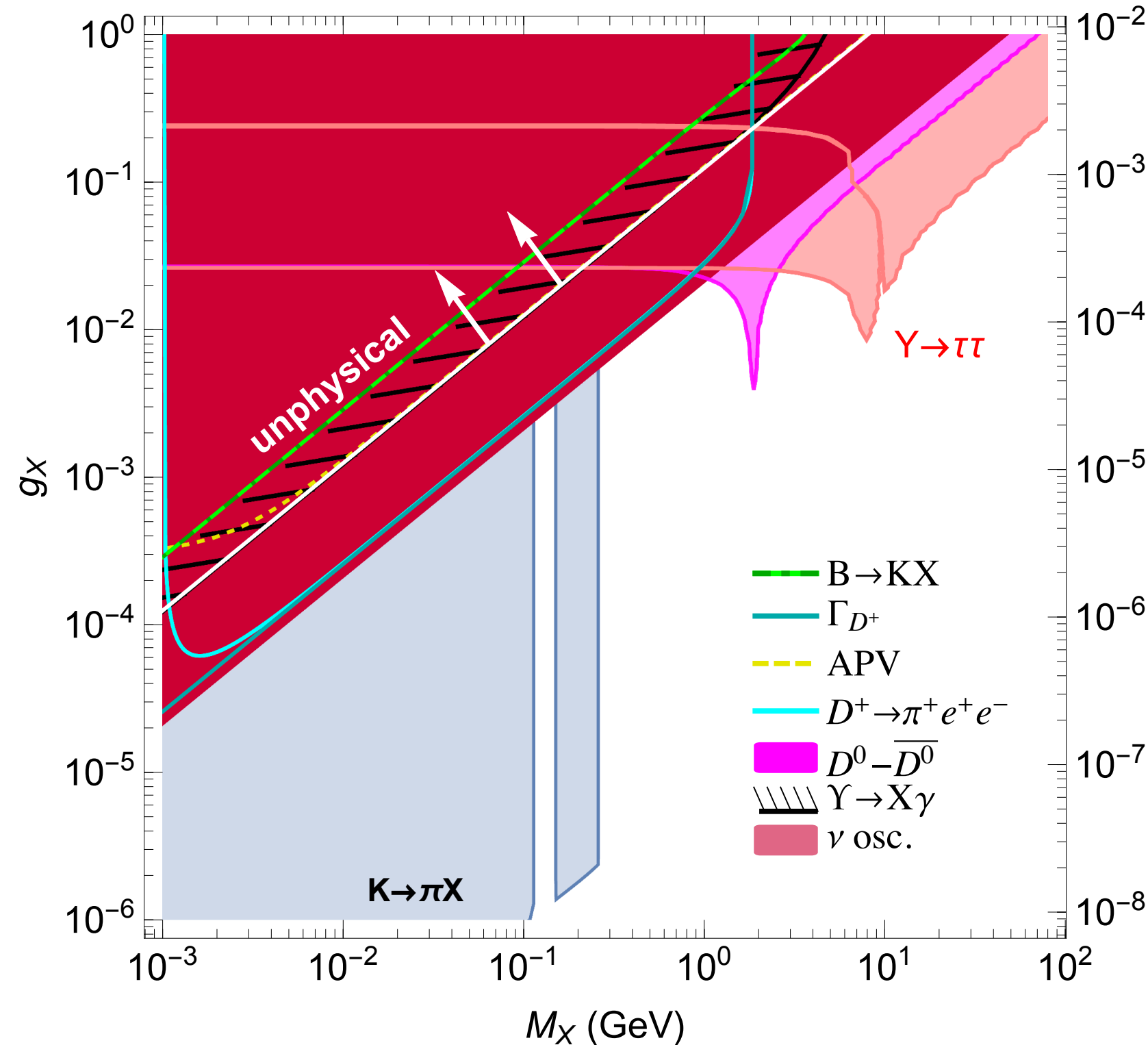
Hadronic cross section:

$$\Gamma(X \rightarrow \text{hadrons}) = \Gamma(X \rightarrow \mu^+\mu^-) R(s = M_X^2)$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons}; s)}{\sigma(e^+e^- \rightarrow \mu^+\mu^-; s)}$$

# Flavor Physics

$$\tan\beta = v_2/v_1 = 10$$



**U(1) B – L of the third family**

Complete model, including scalar sector and CKM generation



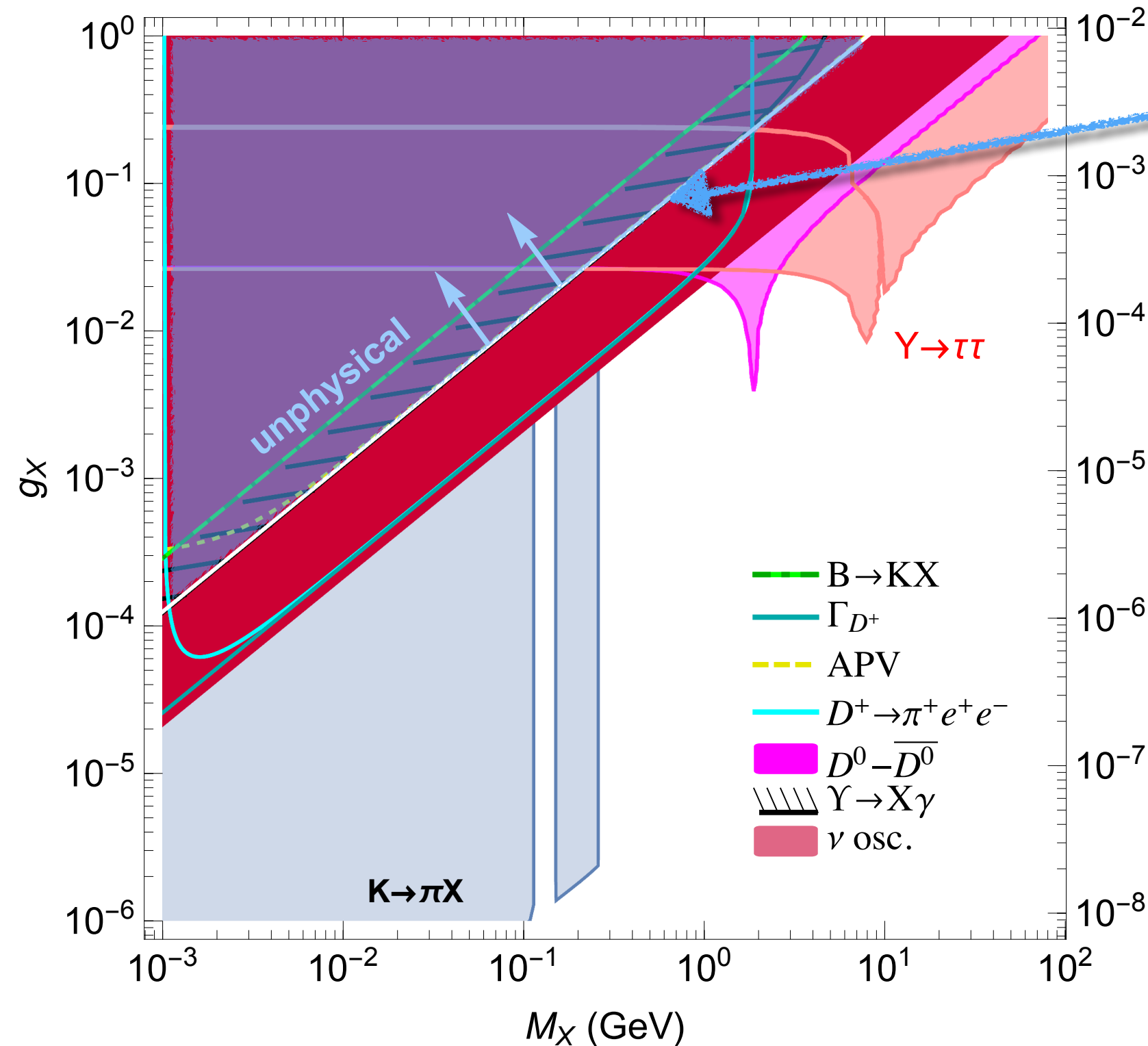
$$Z_\mu \simeq -s_w B_\mu + c_w W_\mu^3 - s_X X_\mu^0,$$

$$X_\mu \simeq s_X (-s_w B_\mu + c_w W_\mu^3) + X_\mu^0,$$

$$s_X \equiv \frac{2}{3} \frac{g_X}{\sqrt{g^2 + g'^2}} \frac{v_1^2}{v^2}$$

# Flavor Physics

$$\tan\beta = v_2/v_1 = 10$$



$$M_X^2 = \frac{1}{9} g_X^2 \left( \frac{v_1^2 v_2^2}{v^2} + v_s^2 \right)$$

$\tan\beta$  fixes  $v_1$  and  $v_2$   
 $M_X$  has a lower value

$s_X$

$$Z_\mu \simeq -s_w B_\mu + c_w W_\mu^3 - s_X X_\mu^0,$$

$$X_\mu \simeq s_X (-s_w B_\mu + c_w W_\mu^3) + X_\mu^0,$$

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# Flavor Physics

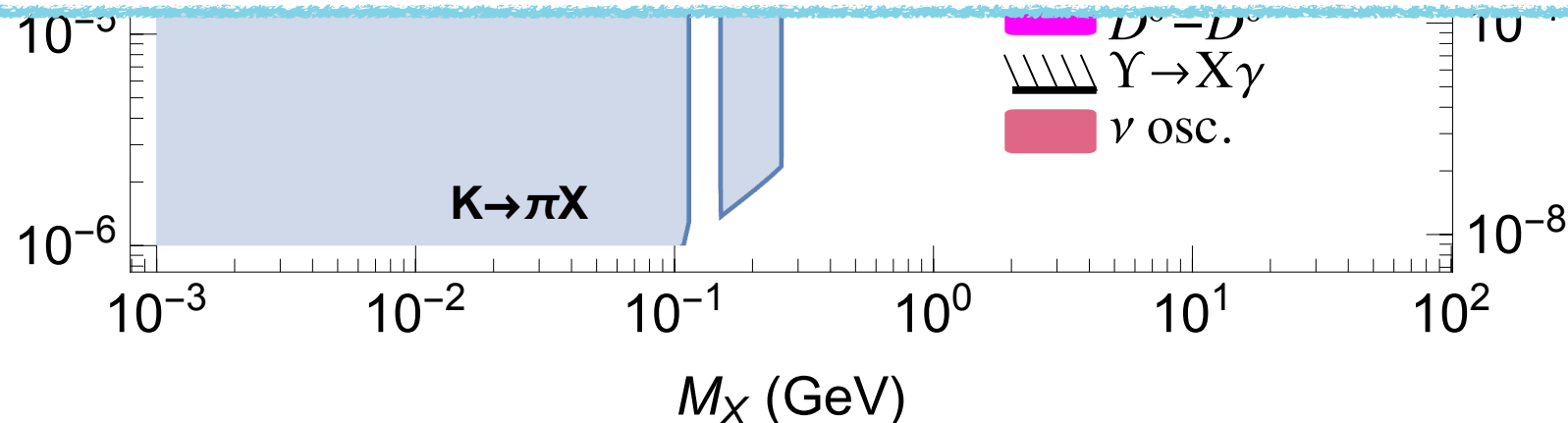
$$\tan\beta = v_2/v_1 = 10$$

At high energies, external longitudinal modes can be replaced by the Goldstone boson associated with the breaking of the symmetry (Equivalence theorem)

$$G_X = \frac{1}{3} \frac{g_X}{M_X v^2} \left[ -v_1 v_2^2 \text{Im}(\phi_1^0) + v_1^2 v_2 \text{Im}(\phi_2^0) - v^2 v_s \text{Im}(s^0) \right]$$

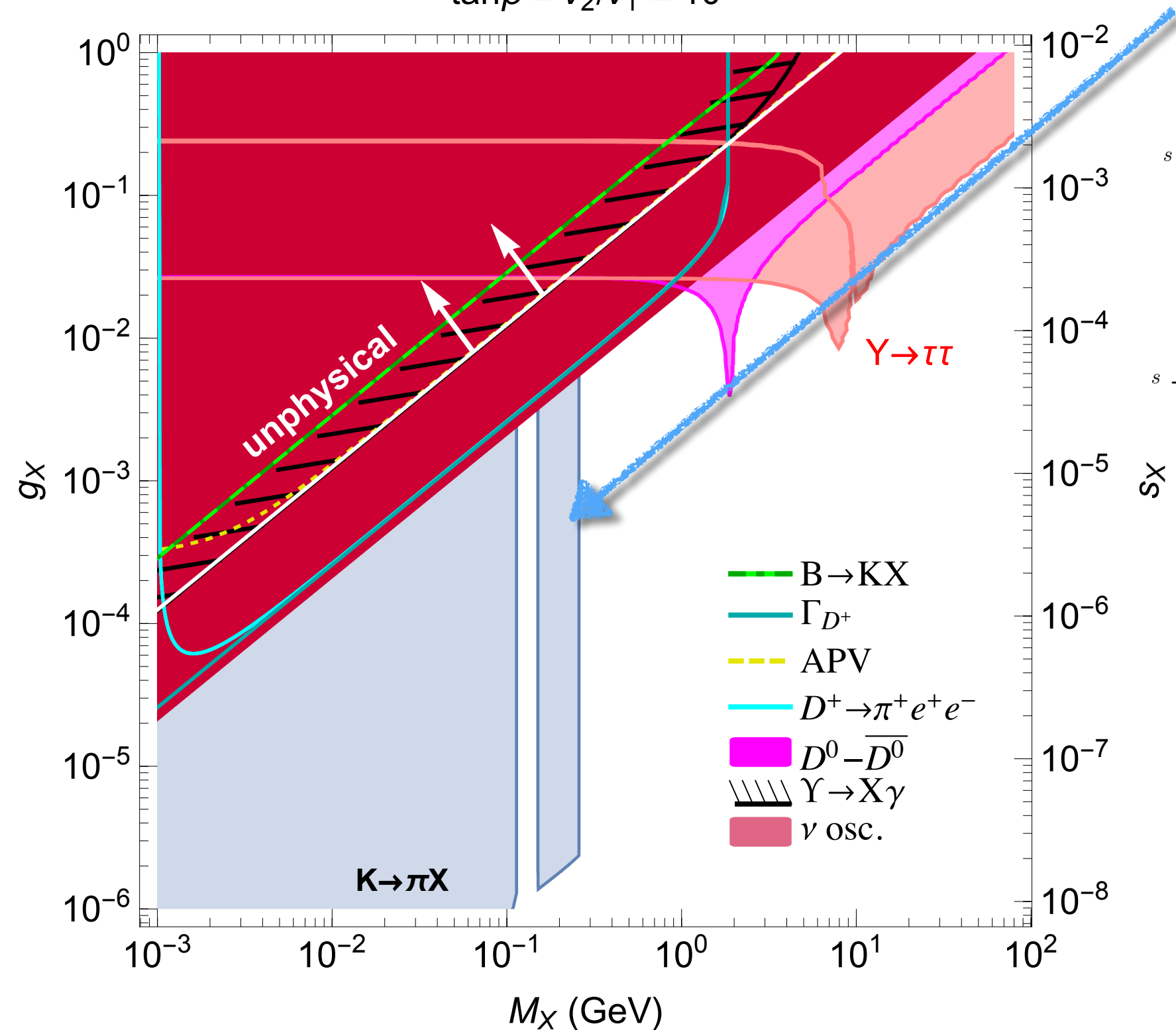
$$\mathcal{L}_{G_X} = iG_X \frac{g_X}{3} \frac{m_t}{M_X} \left[ -\frac{v_1^2}{v^2} \bar{t} \gamma_5 t + V_{cb} (\bar{c}_L t_R - \bar{t}_R c_L) + V_{ub} V_{cb} (\bar{c}_L u_R - \bar{u}_R c_L) \right] - iG_X \frac{g_X}{3} \frac{m_\tau}{M_X} \frac{v_1^2}{v^2} \bar{\tau} \gamma_5 \tau + \dots$$

$$\mathcal{L}_{hXX} = \frac{g_X^2}{9} \frac{v_1^2 v_2^2}{v^3} \text{Re}(H^0) X_\mu X^\mu$$



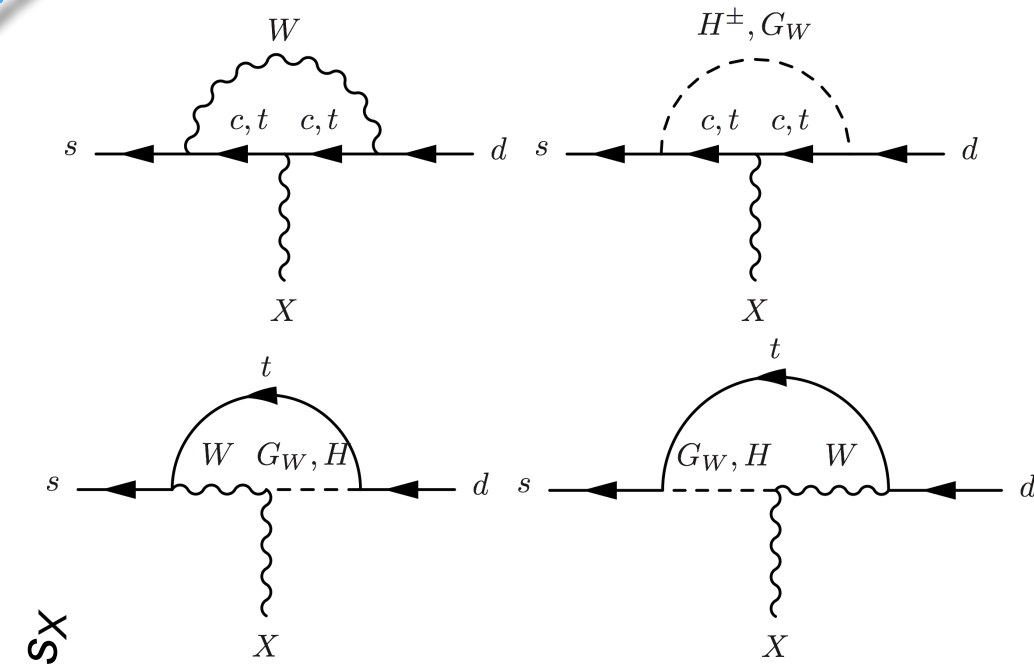
# Flavor Physics

$$\tan\beta = v_2/v_1 = 10$$



$$K \rightarrow \pi X \rightarrow \pi \nu \nu$$

Longitudinal enhancement

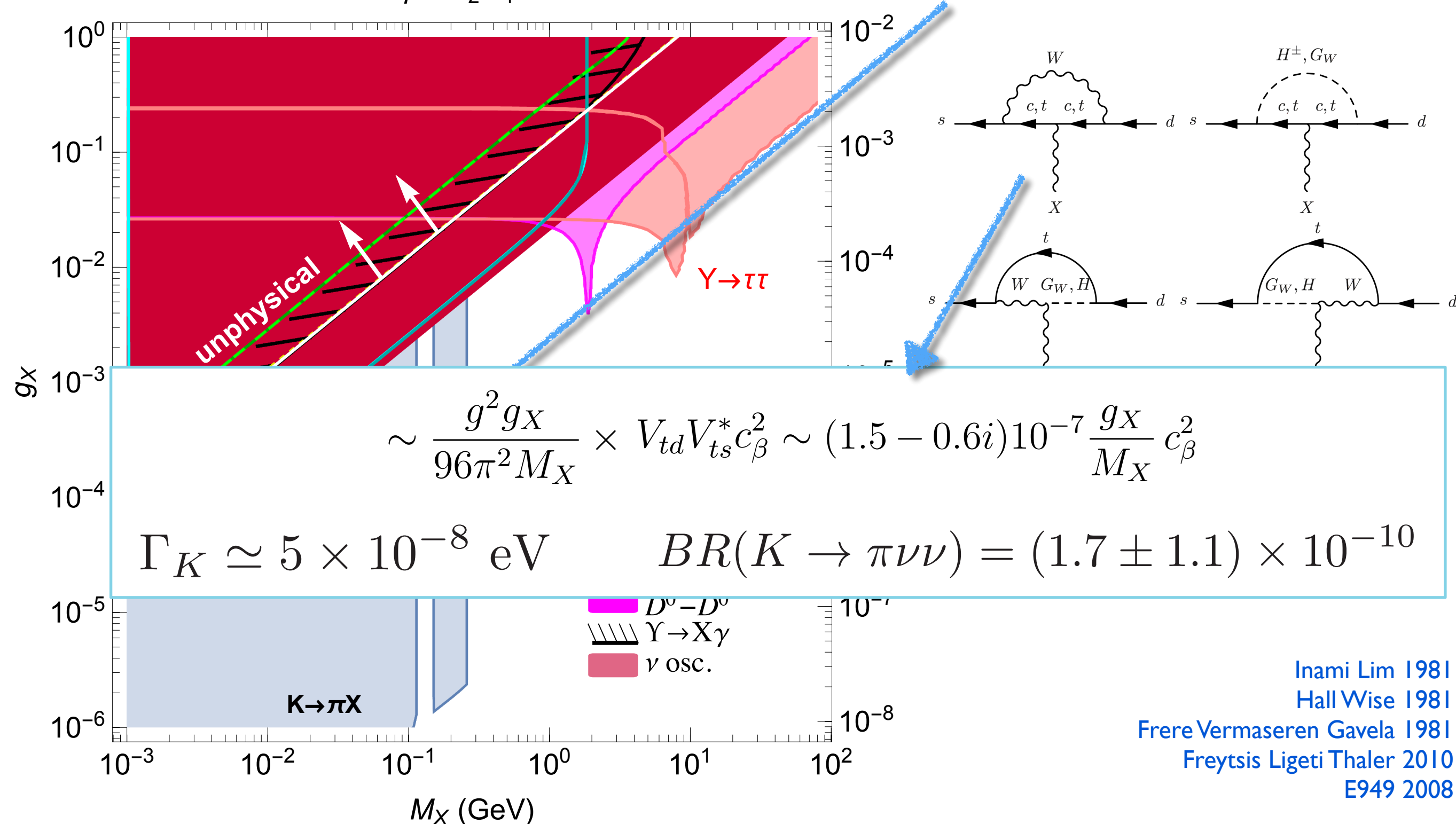


Inami Lim 1981  
 Hall Wise 1981  
 Frere Vermaseren Gavela 1981  
 Freytsis Ligeti Thaler 2010  
 E949 2008

# Flavor Physics

$$\tan\beta = v_2/v_1 = 10$$

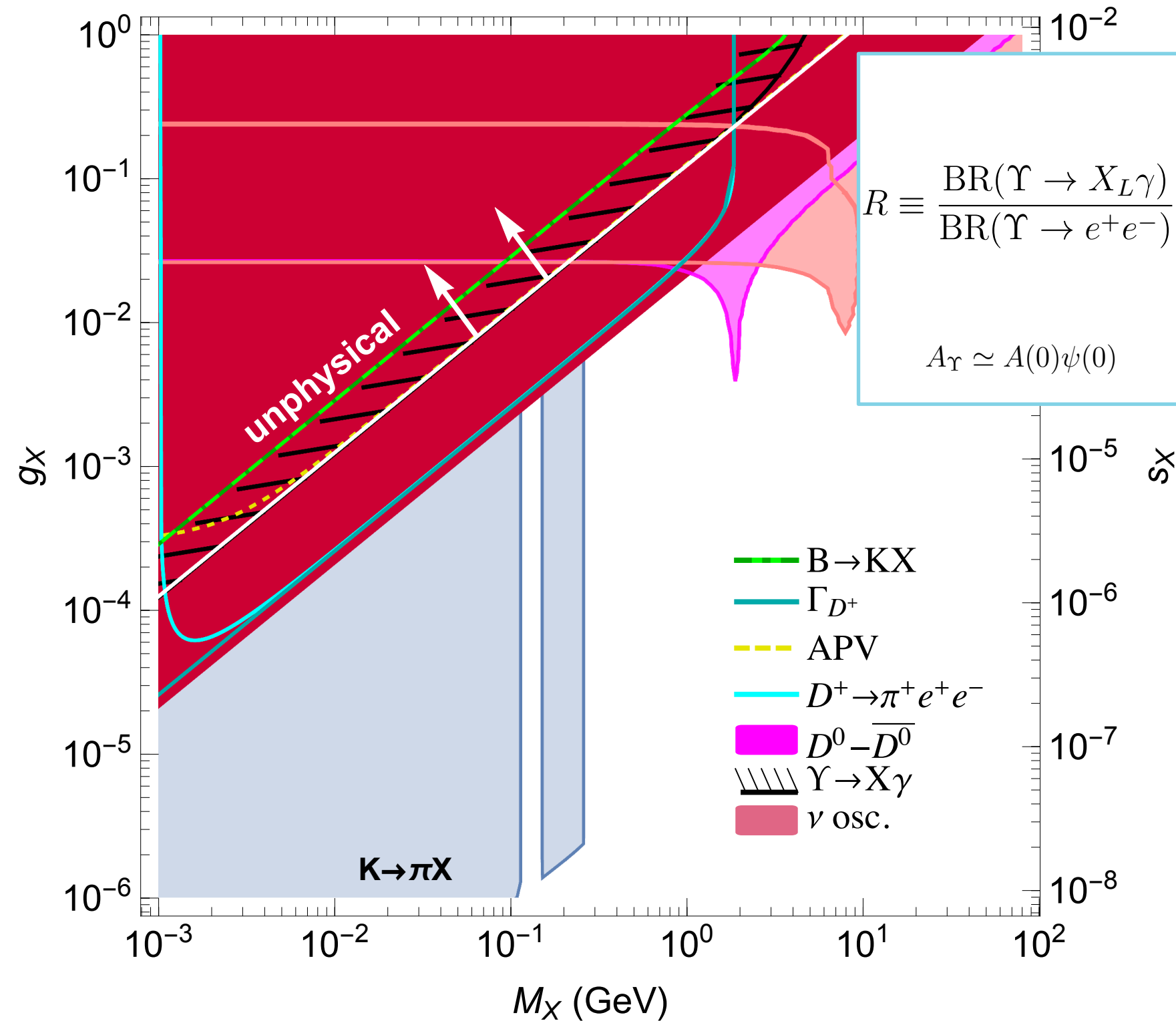
$K \rightarrow \pi X \rightarrow \pi \nu\nu$   
Longitudinal enhancement



# $\Upsilon$ to $X\gamma$

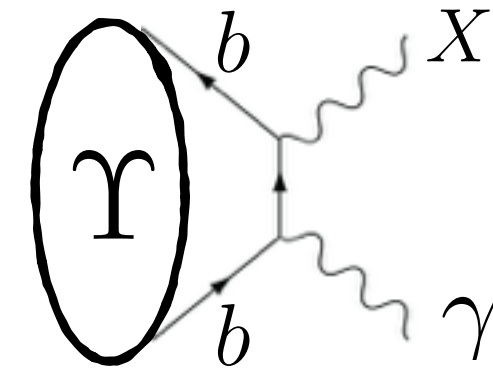
Longitudinal enhancement

$$\tan\beta = v_2/v_1 = 10$$



$$R \equiv \frac{\text{BR}(\Upsilon \rightarrow X_L \gamma)}{\text{BR}(\Upsilon \rightarrow e^+ e^-)} = \frac{|\psi(0)|^2 |A(0; b\bar{b} \rightarrow X_L \gamma)|^2}{|\psi(0)|^2 |A(0; b\bar{b} \rightarrow e^+ e^-)|^2} \simeq \frac{2g_X^2 v_1^4 m_b^2}{9e^2 v^4 M_X^2}$$

$A_\Upsilon \simeq A(0)\psi(0)$       Yang's theorem



$D^0 - \bar{D}^0$

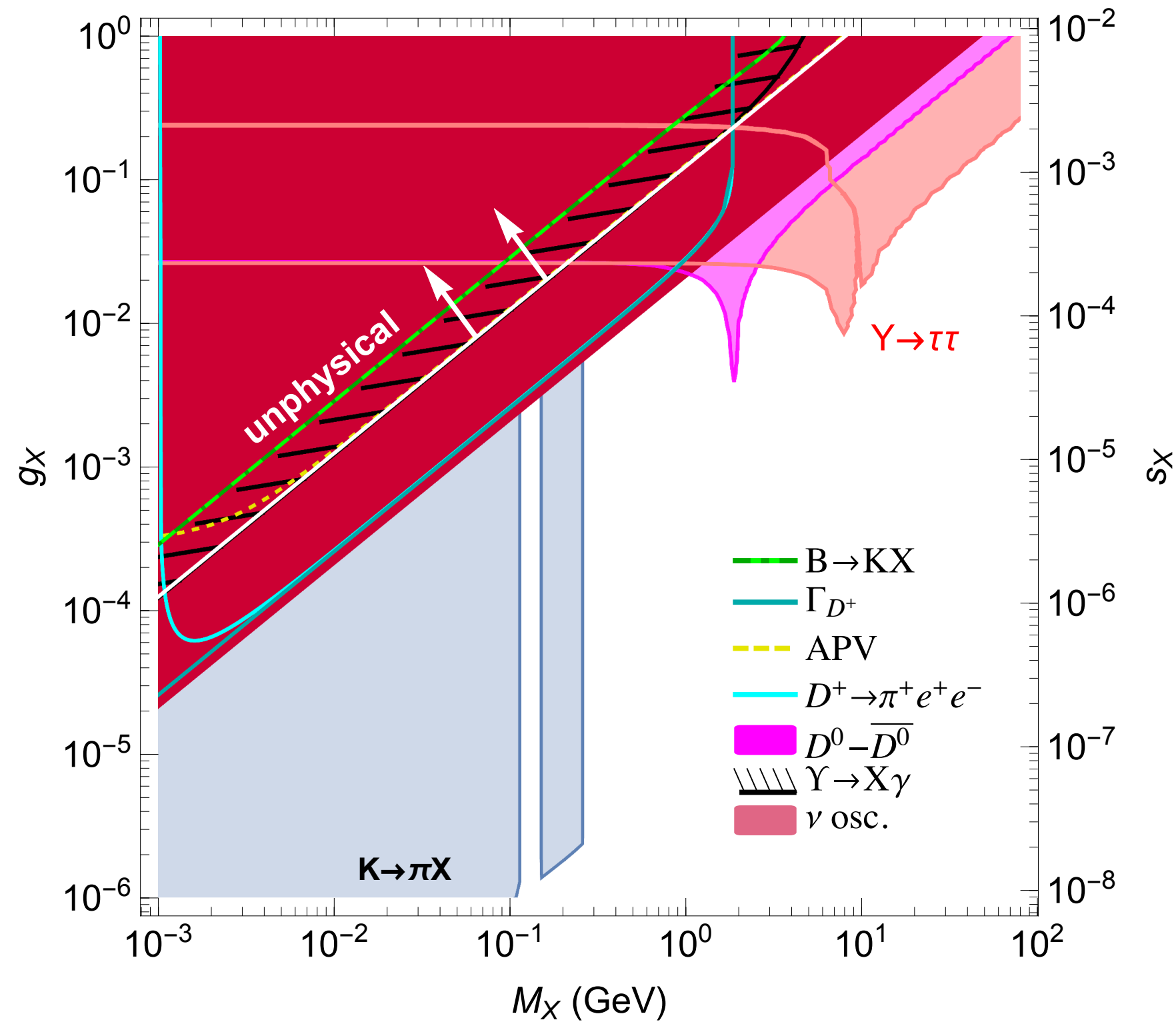
$$\mathcal{L}_{\text{eff}} = C(q^2) (\bar{u}_L \gamma_\mu c_L)^2$$

$$C(q^2) = \frac{g_X^2}{9} \frac{|V_{ub} V_{cb}|^2}{q^2 - M_X^2}$$

$$C(m_D^2) < \frac{5.9 \times 10^{-7}}{\text{TeV}^2}$$



$$\tan\beta = v_2/v_1 = 10$$



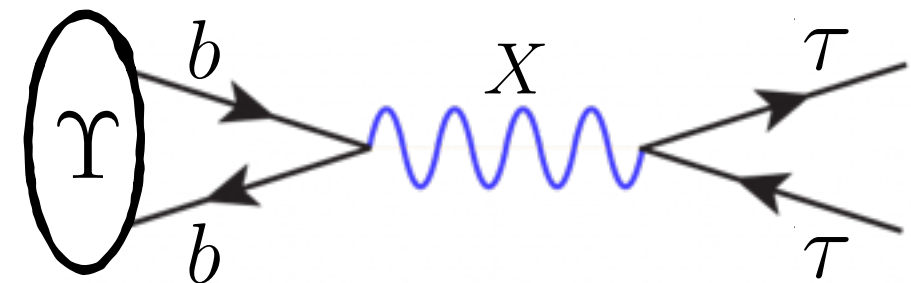
## $\Upsilon$ to $\tau\tau$

Only third family couplings

$$R_{\tau\mu} \equiv \frac{\Gamma(\Upsilon(1S) \rightarrow \tau^+\tau^-)}{\Gamma(\Upsilon(1S) \rightarrow \mu^+\mu^-)}$$

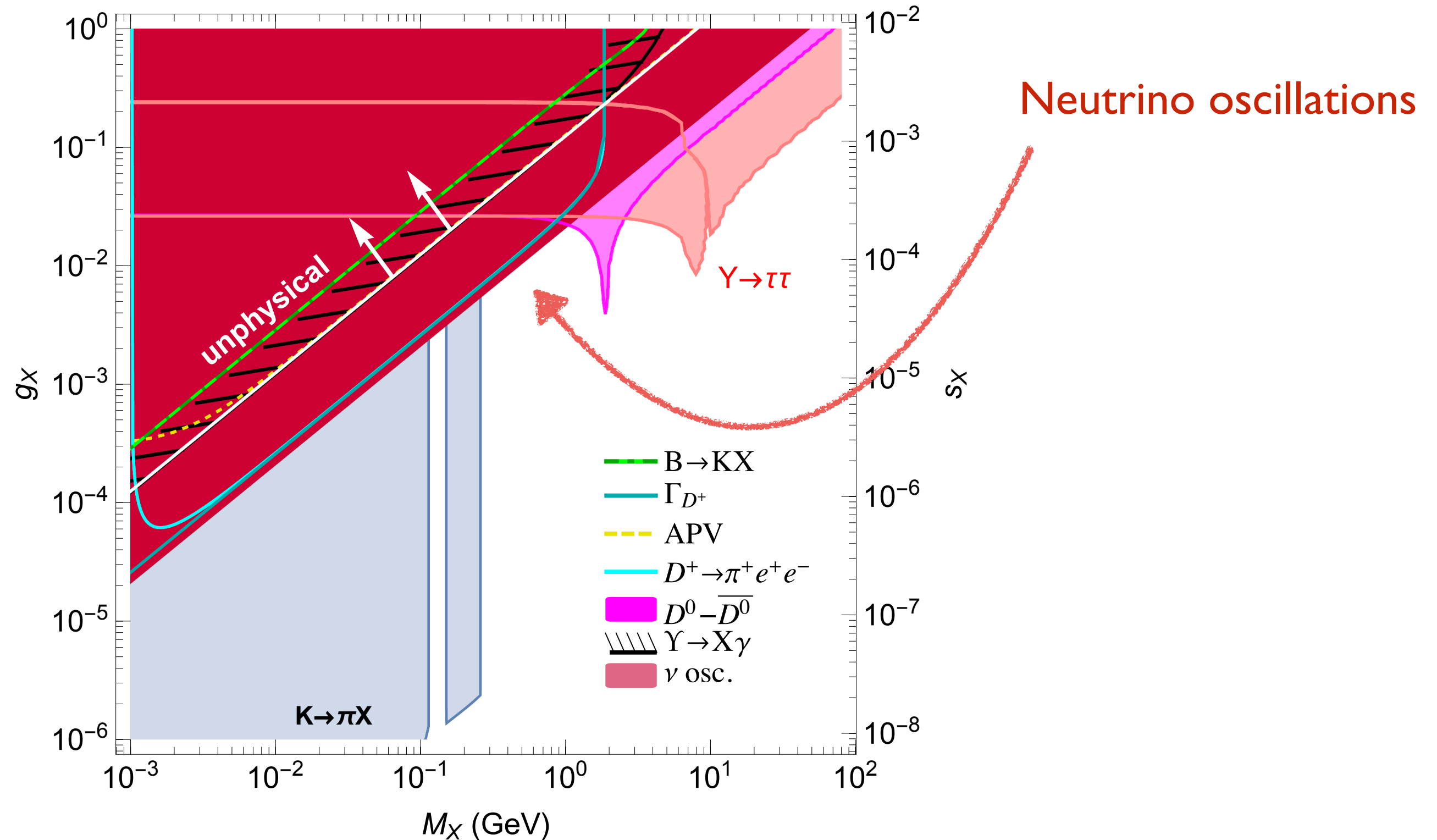
$$1.005 \pm 0.013(\text{stat.}) \pm 0.022(\text{syst.})$$

$$R_{\tau\mu} \simeq 1 - 2 \frac{g_X^2}{e^2} \frac{M_\Upsilon^2}{M_\Upsilon^2 - M_X^2}$$



# Flavor Physics

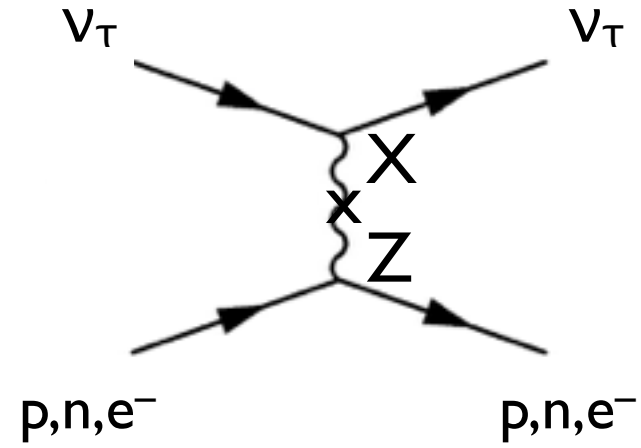
$$\tan\beta = v_2/v_1 = 10$$



Neutrino oscillations

# Flavor Physics

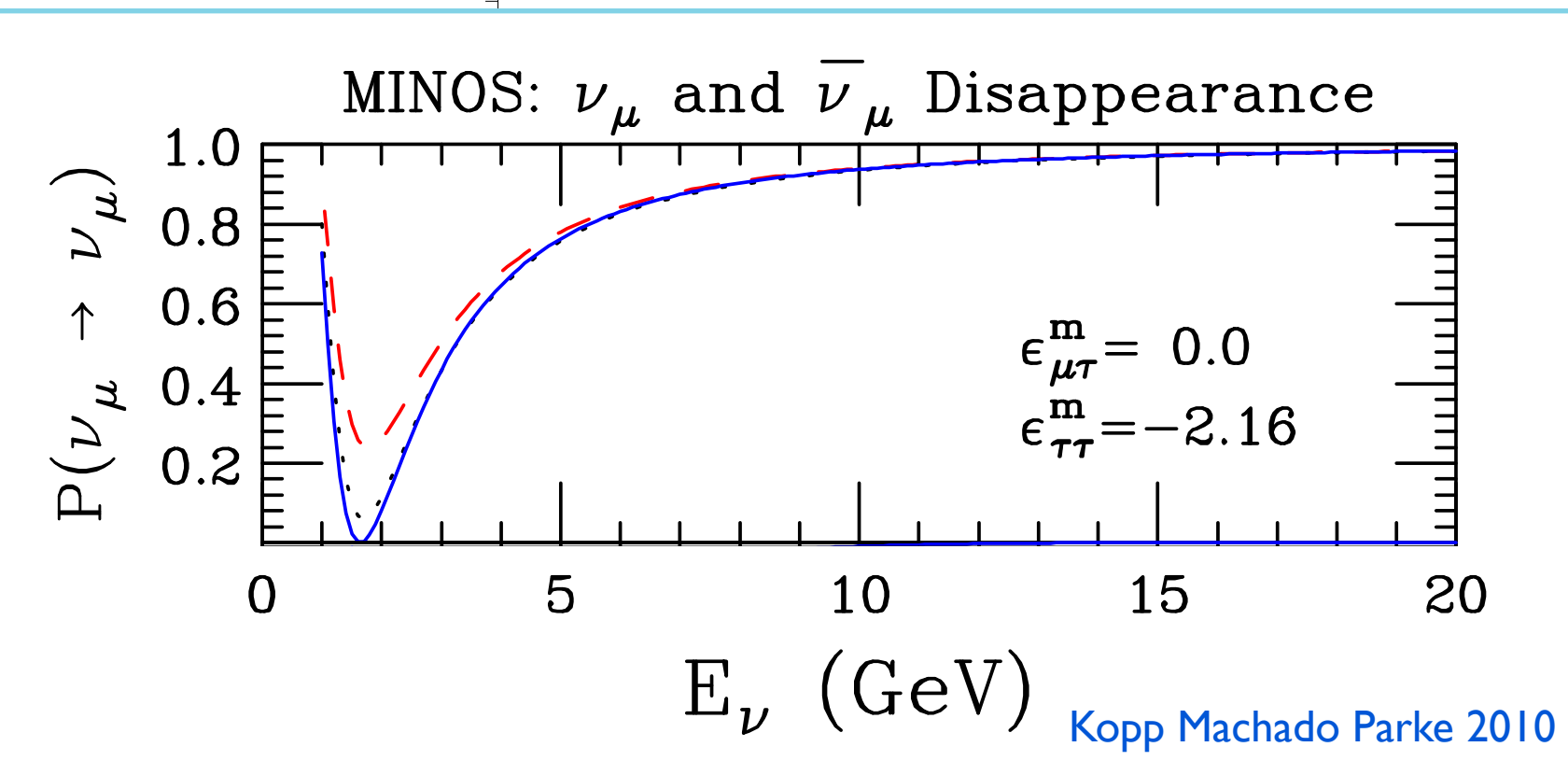
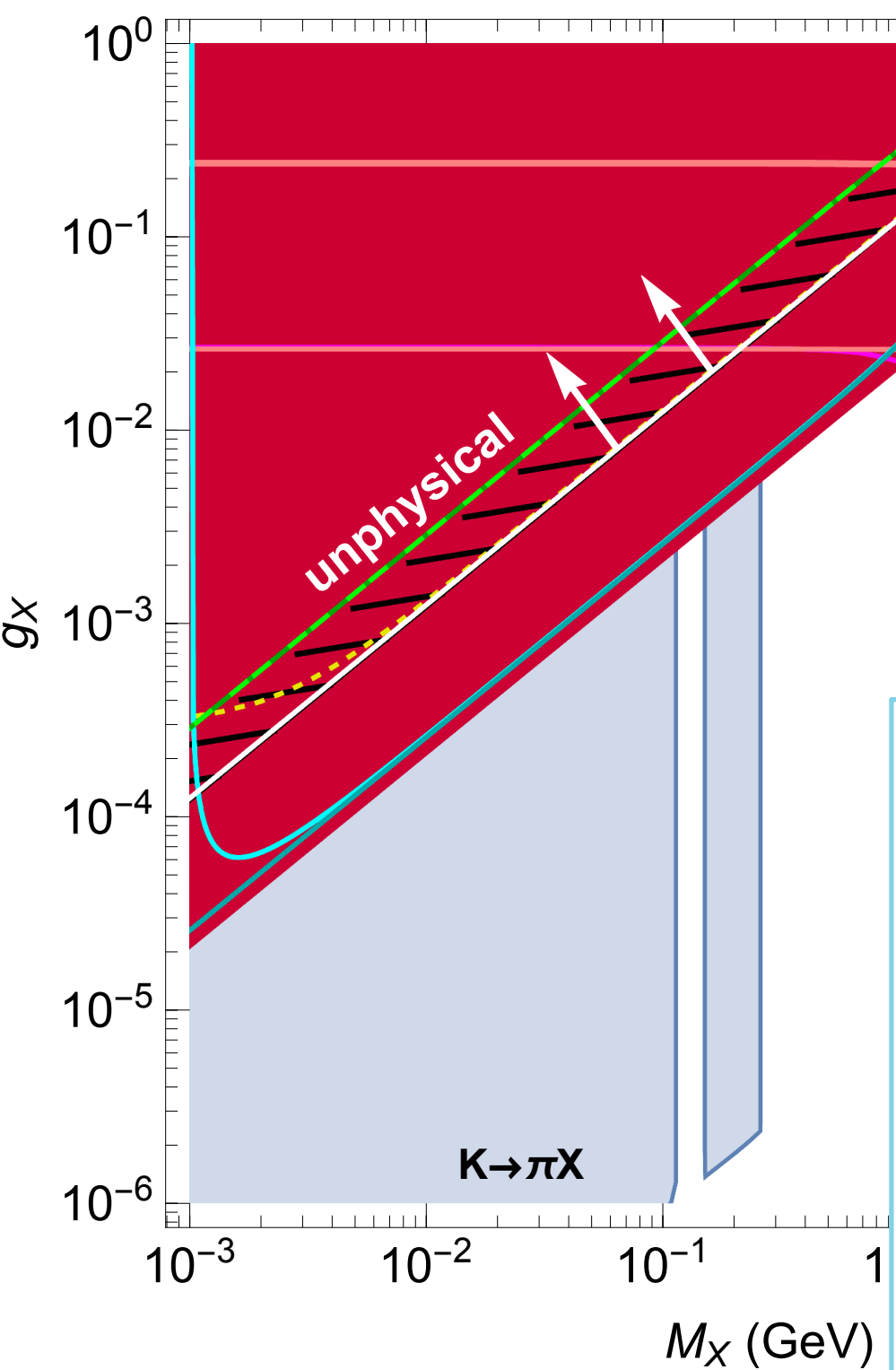
$$\tan\beta = v_2/v_1 = 10$$



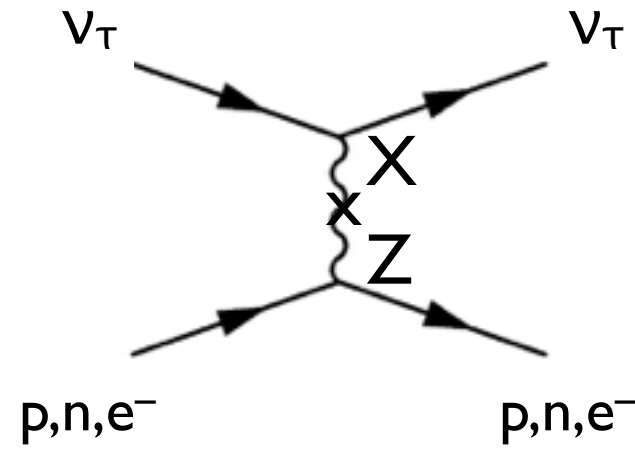
$$2\sqrt{2}G_F\varepsilon_{\alpha\alpha}^f (\bar{\nu}_{\alpha L}\gamma_\mu\nu_{\alpha L}) (\bar{f}\gamma^\mu f)$$

$$\varepsilon_{\tau\tau} \equiv \varepsilon_{\tau\tau}^p + \varepsilon_{\tau\tau}^n + \varepsilon_{\tau\tau}^e = 3 \frac{v_1^2 v^2}{v_1^2 v_2^2 + v_s^2 v^2}$$

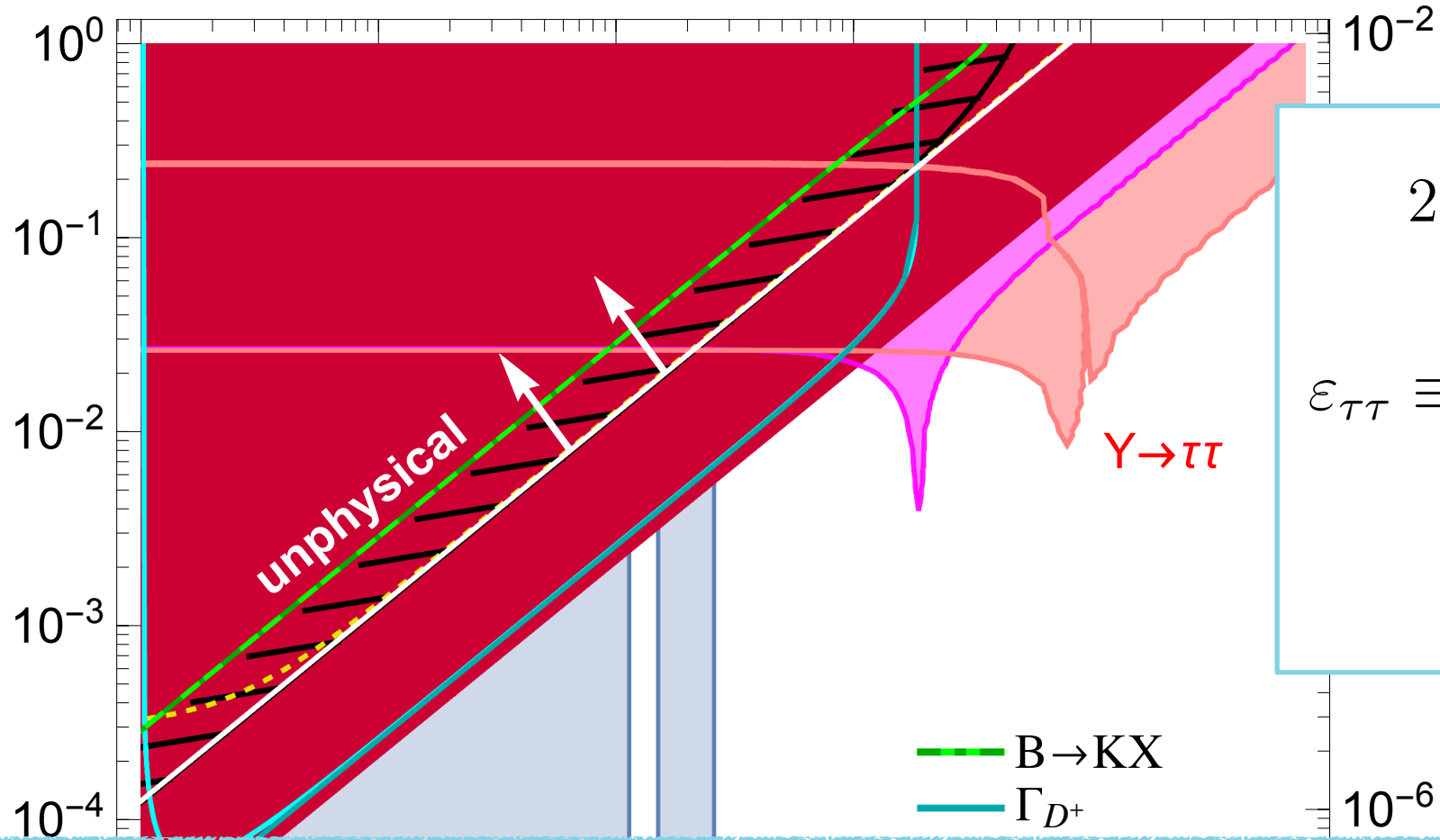
$$|\varepsilon_{\tau\tau}| < 0.09$$



# Flavor Physics



$$\tan\beta = v_2/v_1 = 10$$



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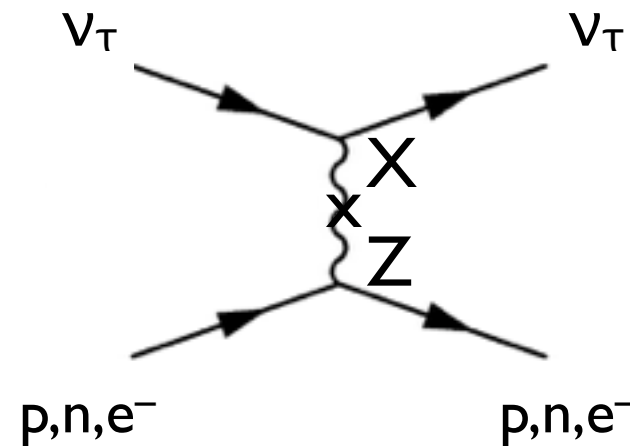
The third family is not special!

Matter potential  $\longrightarrow$  symmetry breaking scale

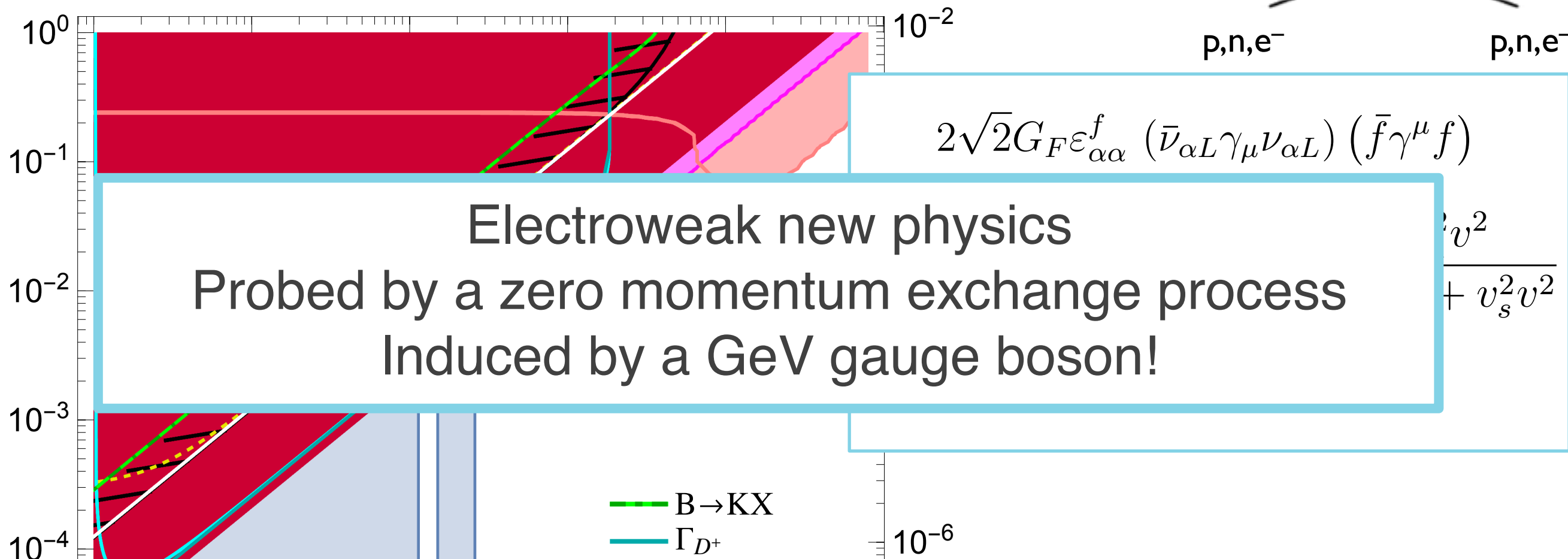
$$V_{CC} = \sqrt{2}G_F N_e, \quad G_F = \frac{1}{\sqrt{2}v^2}$$

NSI:  $2\sqrt{2}G_F\varepsilon_{\alpha\alpha}^f (\bar{\nu}_{\alpha L}\gamma_\mu\nu_{\alpha L}) (\bar{f}\gamma^\mu f) \longrightarrow$  1% NSI translate into  $v' \sim 10v$

# Flavor Physics



$$\tan\beta = v_2/v_1 = 10$$



The third family is not special!

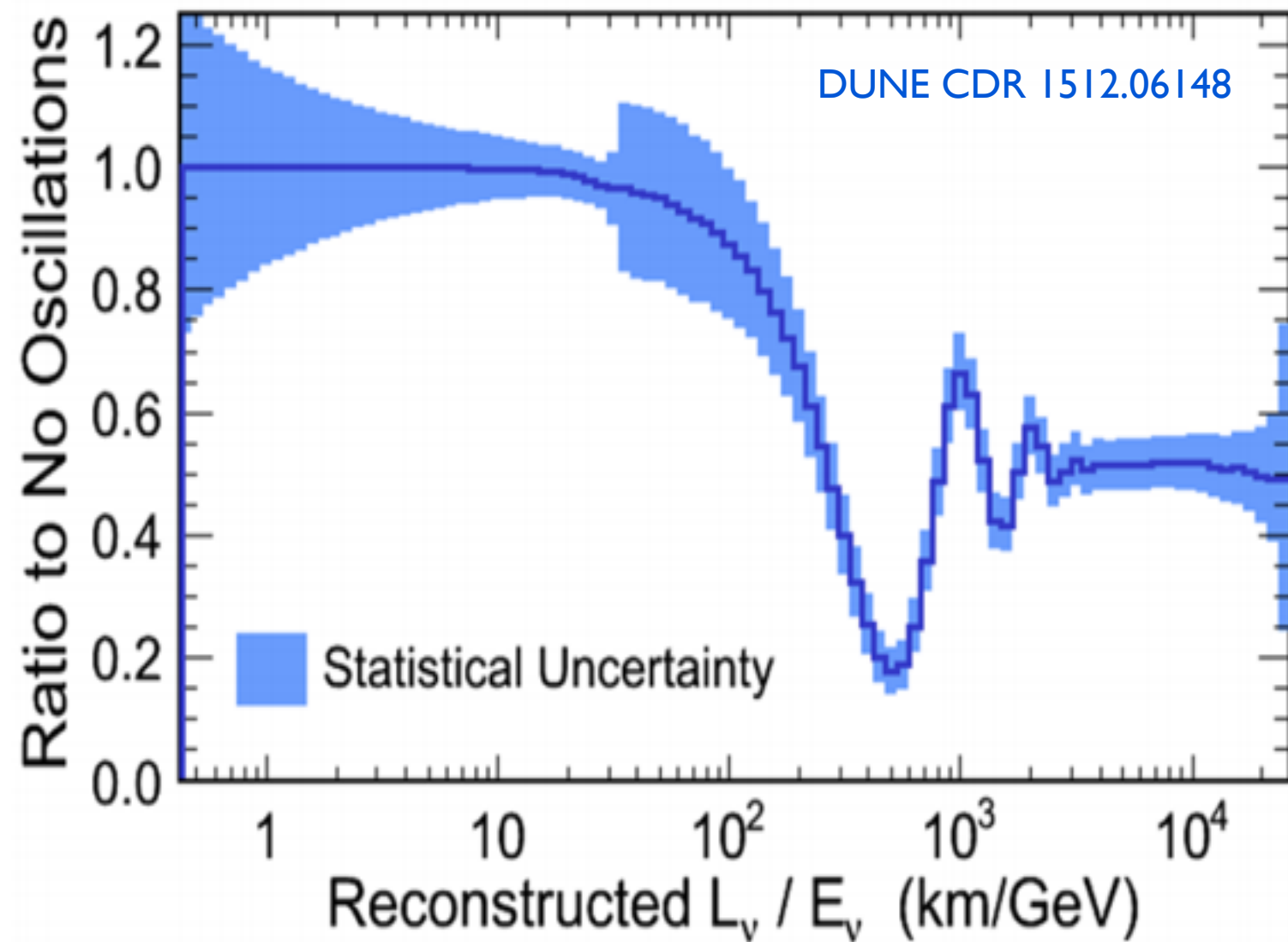
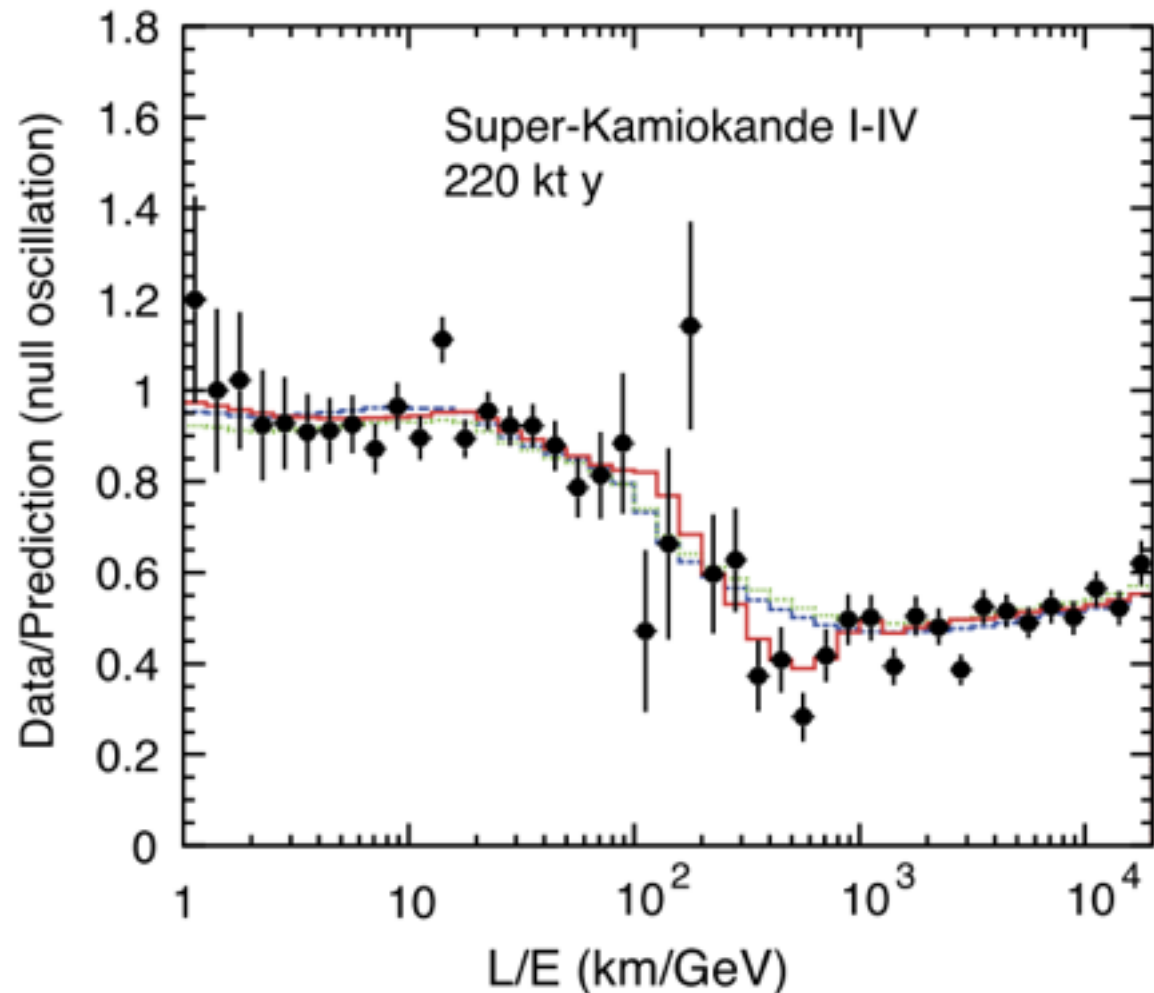
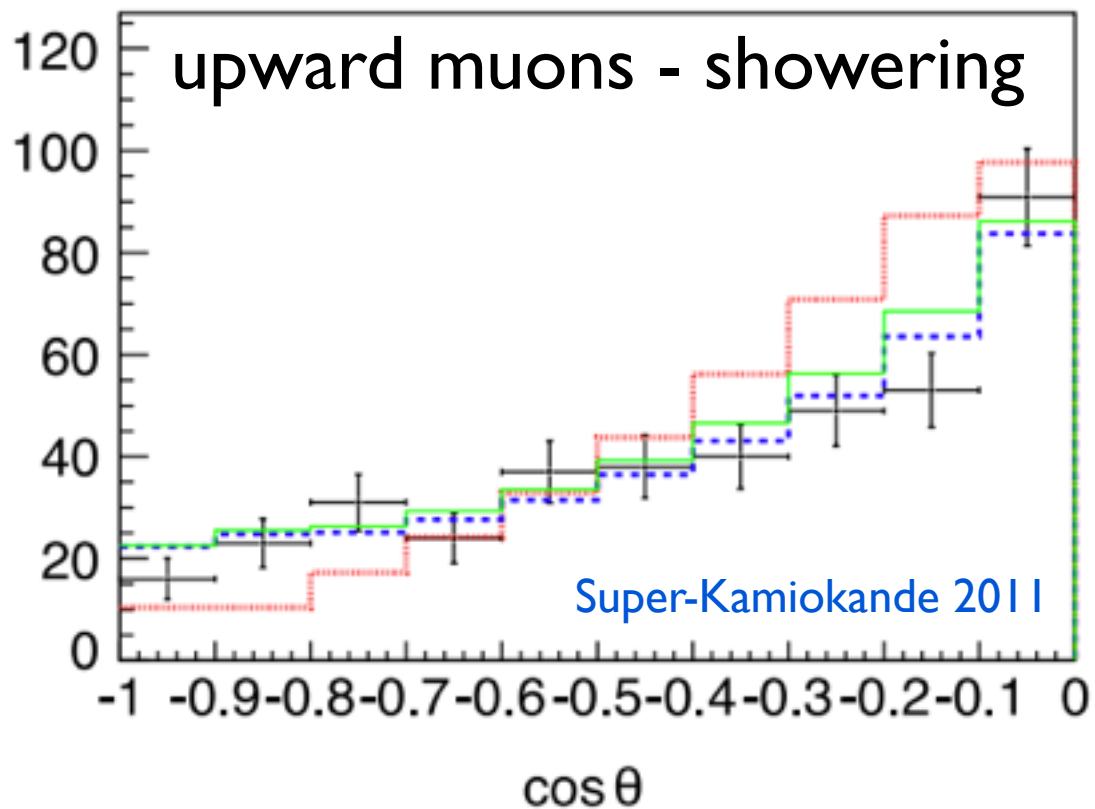
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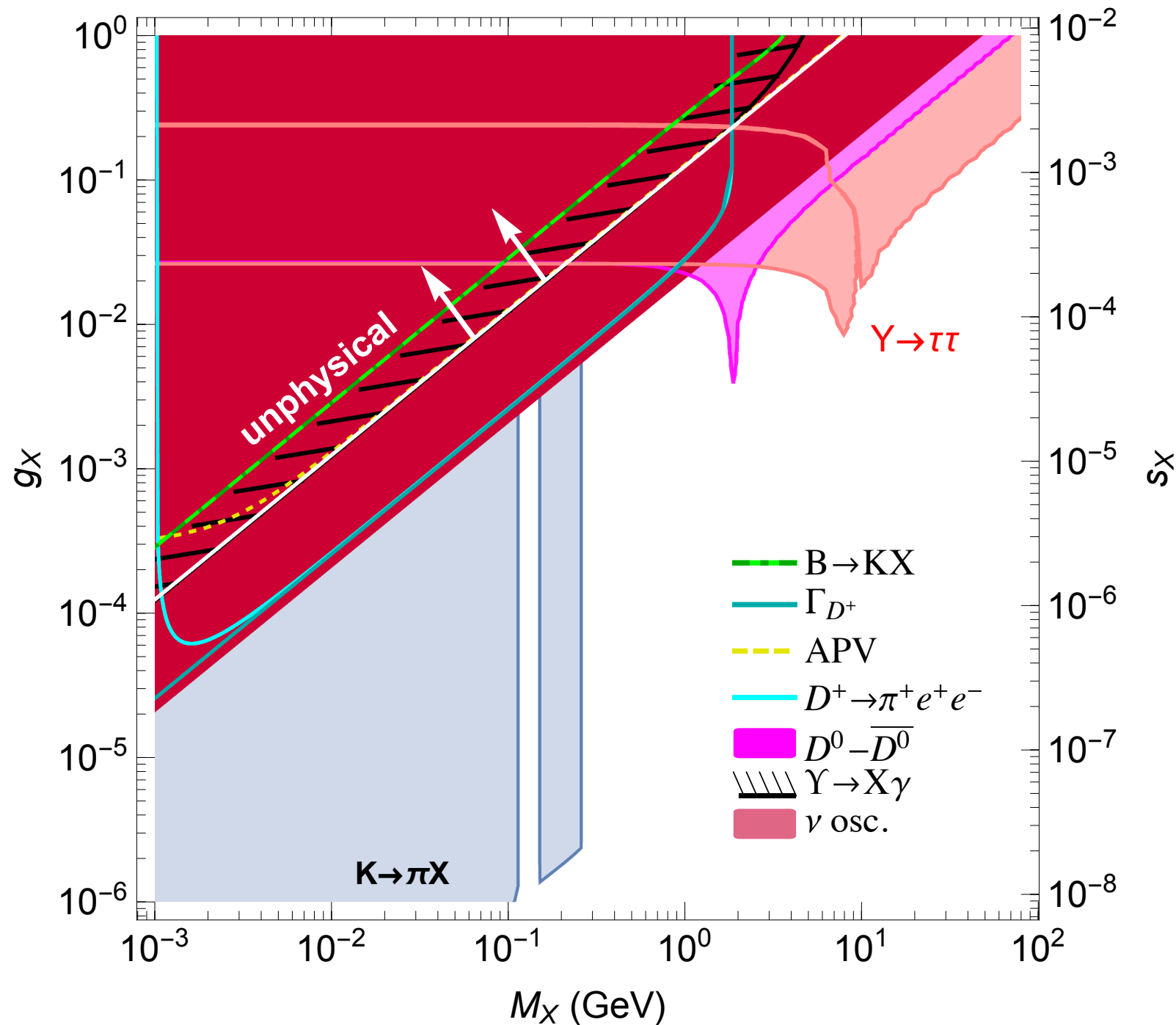
NSI:  $2\sqrt{2}G_F\varepsilon_{\alpha\alpha}^f (\bar{\nu}_{\alpha L}\gamma_\mu\nu_{\alpha L}) (\bar{f}\gamma^\mu f) \longrightarrow$  1% NSI translate into  $v' \sim 10v$

# $\epsilon_{\tau\tau}$ from atmospheric neutrinos: DUNE?

# $\epsilon_{TT}$ from atmospheric neutrinos: DUNE?



$$\tan\beta = v_2/v_1 = 10$$



**Top decays**  
longitudinal enhancement

**X at the LHC**  
Non-standard Z' search

**Meson oscillation**  
Probing FCNCs

**BES-III**  
 $e^+e^-$  to  $\tau^+\tau^-$

**$(g-2)_\mu$**   
Does not decouple, but weak

**Beam dump exps**  
X decays invisibly

**W to  $\tau \nu X$**   
longitudinal + transverse

**LEP direct searches**  
Coupling to  $e^-$

**Upsilon decays**  
X-Z mixing / third family coupling

**Neutrino scattering**  
X-Z mixing

**Møller scattering**  
X-Z mixing

**B, D, K decays**  
X-Z mixing

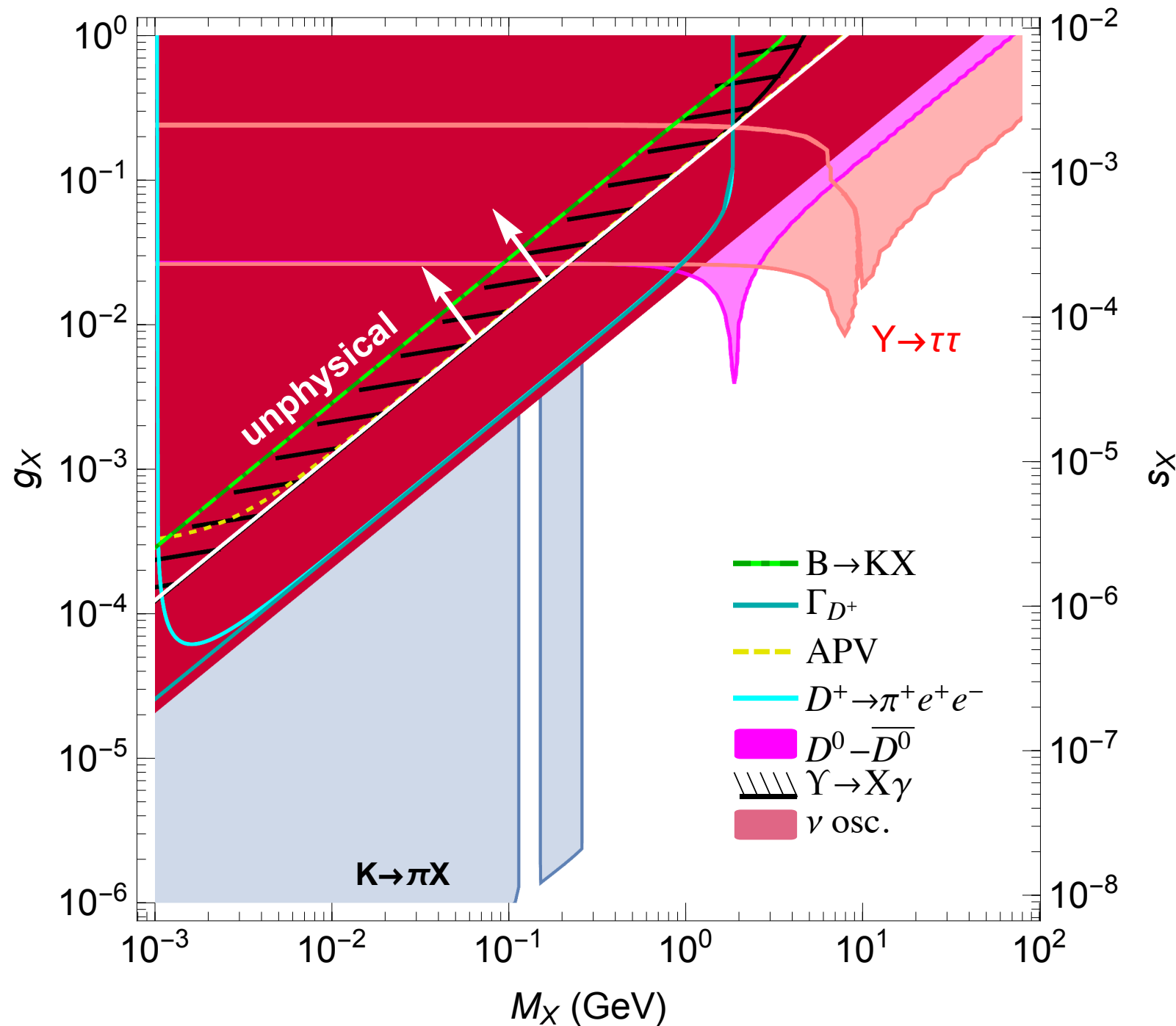
**h invisible decays**  
Longitudinal enhancement

**Z to  $bbX, \tau\tau X$**   
Transverse mode

**Atomic parity violation**  
X-Z mixing



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Transverse mode

**Atomic parity violation**  
X-Z mixing

# Conclusions

## Low scale flavor models

There could be flavor dependent physics below the electroweak scale

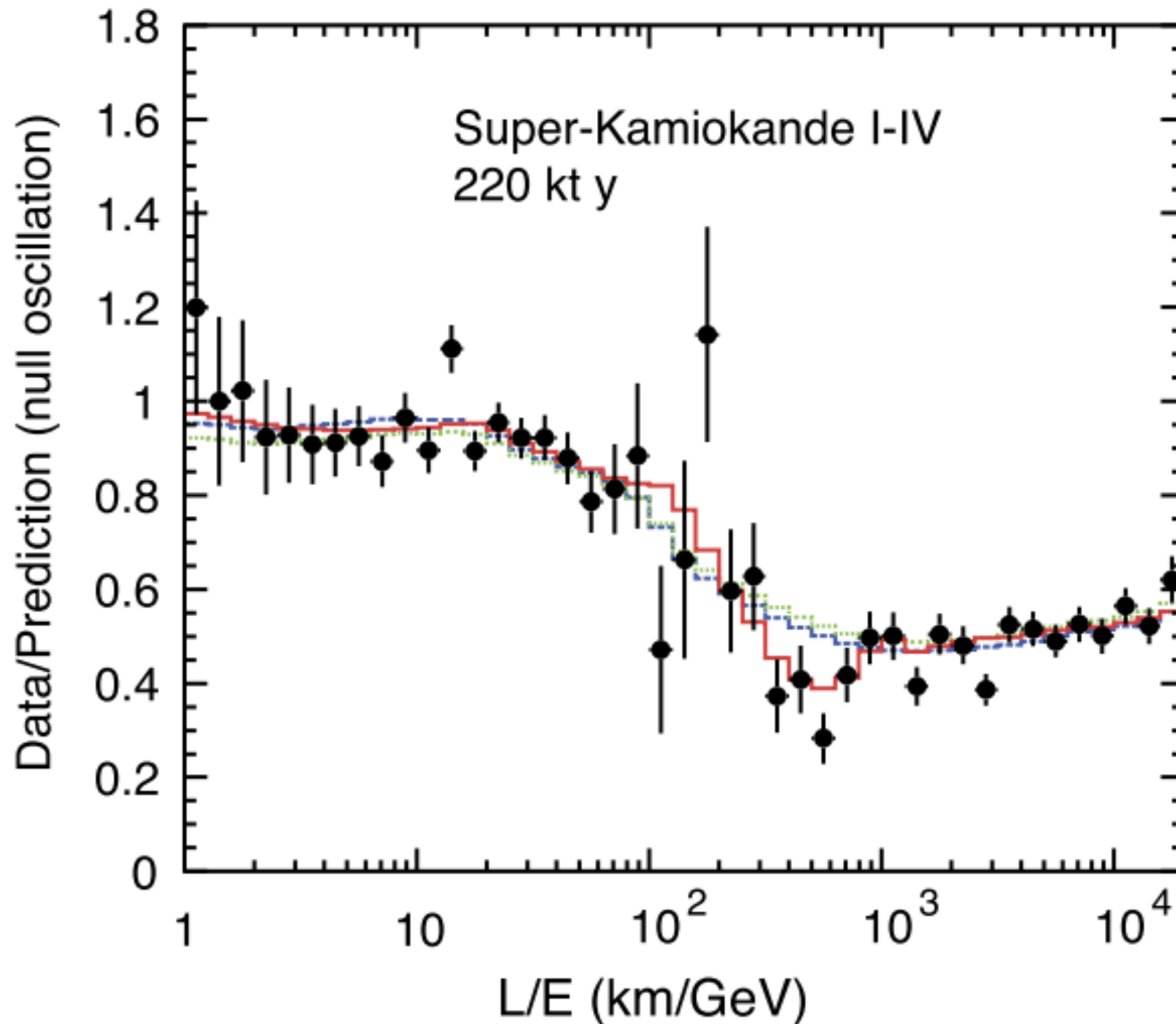
Synergy between vastly different physics: neutrino oscillations, higgs decays, b-physics, APV, meson oscillation and decays...

Neutrinos experiments can be sensitive to physics beyond the reach of collider experiments

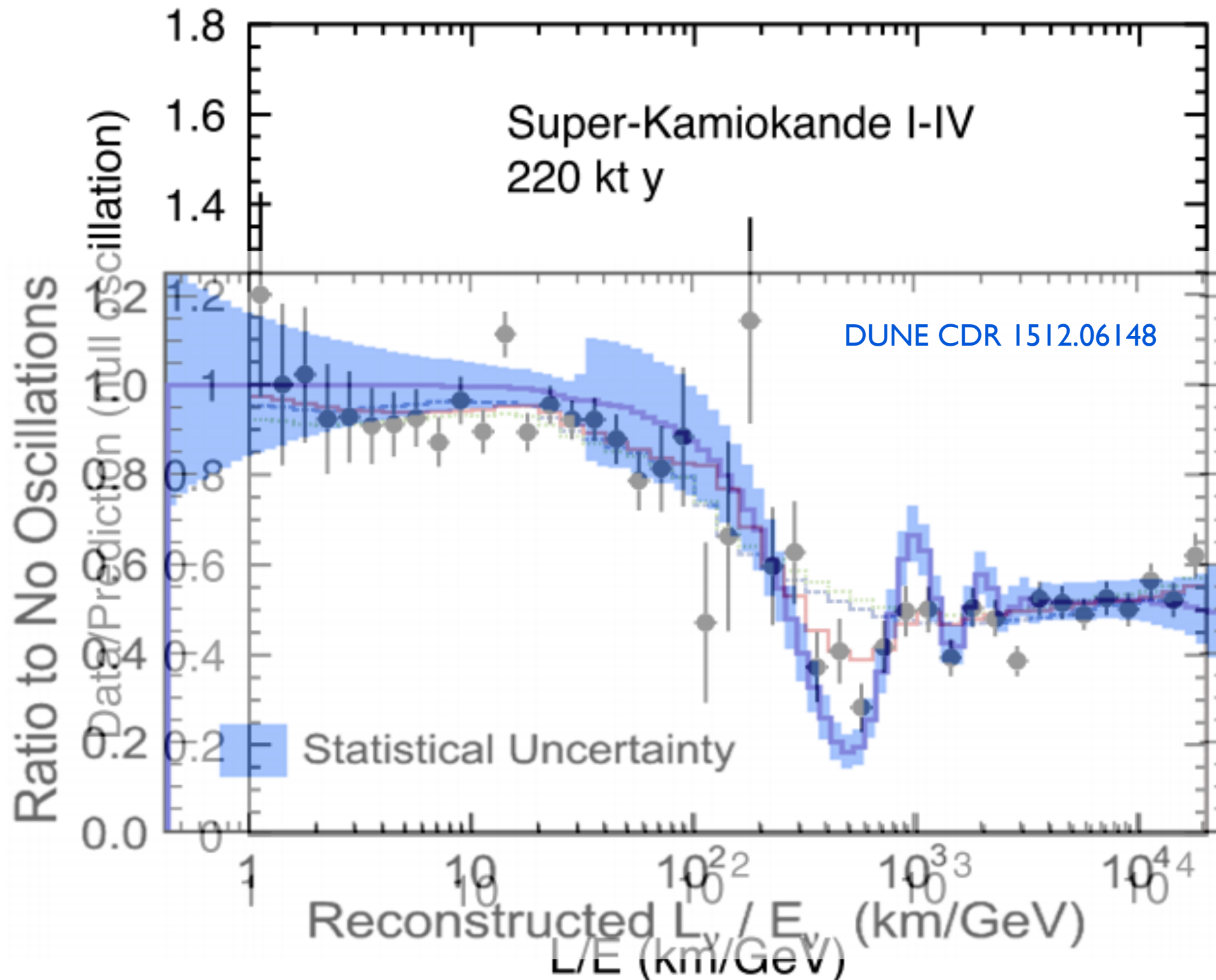
*Do B anomalies point to a flavor dependent new interaction?*

# Backup

Best constraint on  $\epsilon_{\tau\tau}$  comes from atmospheric neutrinos  
Will the current bound be improved by DUNE?

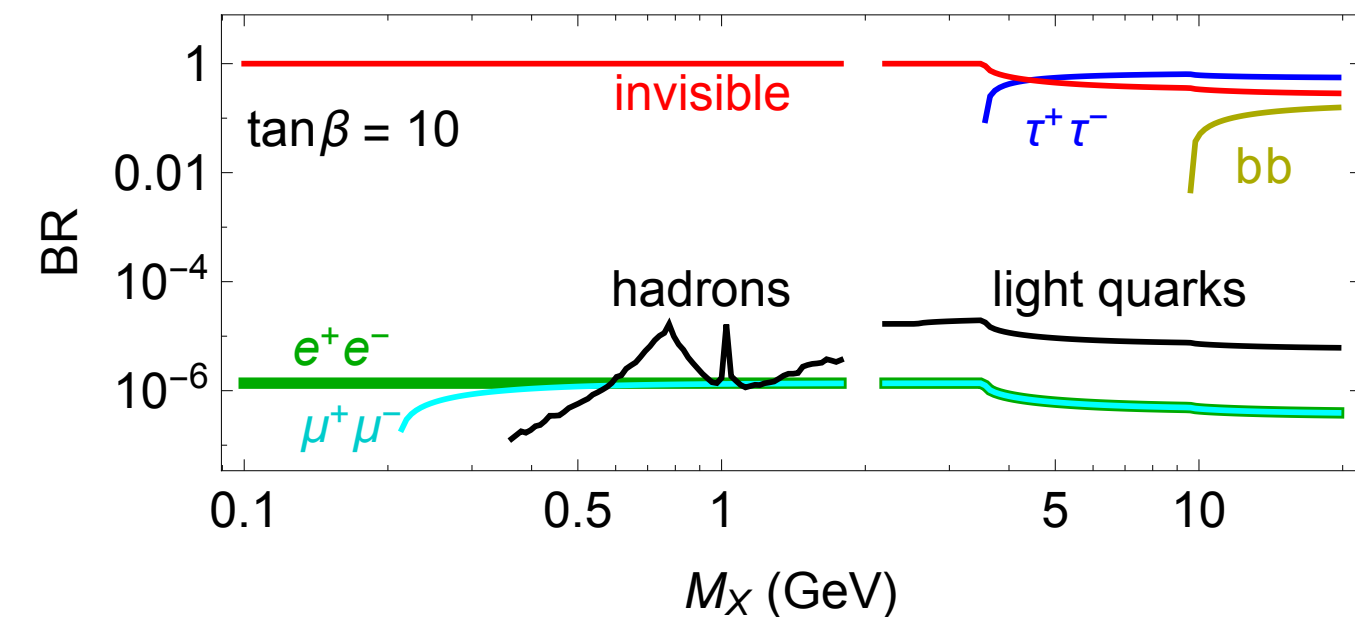
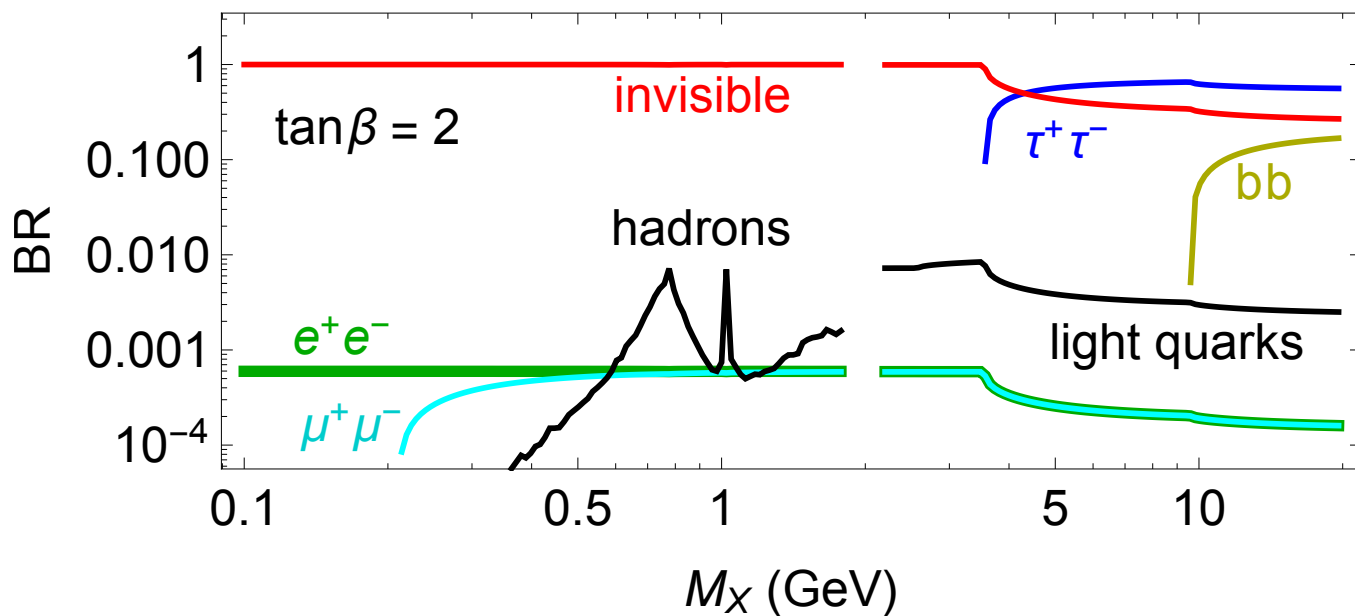


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Will the current bound be improved by DUNE?



$$c_\alpha = q_\alpha c_w e \varepsilon + \left( g_X q_\alpha^X + s_X \sqrt{g^2 + g'^2} q_\alpha^Z \right)$$

Light  $X$ :  $\nu_\tau \nu_\tau$  dominates

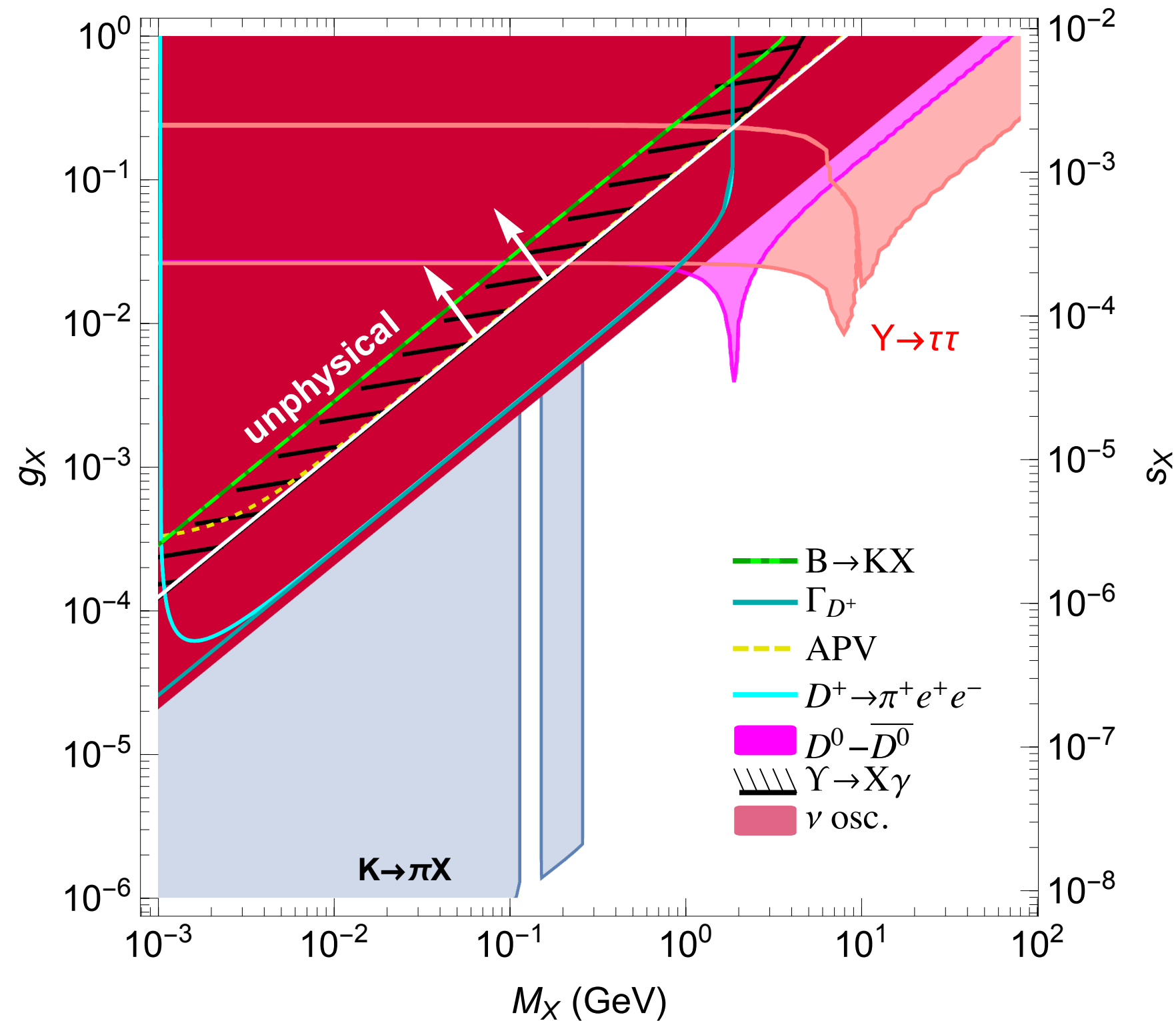


Hadronic cross section:

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$$R(s) = \frac{\sigma(e^+ e^- \rightarrow \text{hadrons}; s)}{\sigma(e^+ e^- \rightarrow \mu^+ \mu^-; s)}$$

$$\tan\beta = v_2/v_1 = 10$$



## Electroweak T parameter

$$\Delta M_Z^2 \simeq \frac{g_X^2 v_1^4}{9 v^2}$$

$$T \simeq \frac{1}{\alpha} \frac{\Delta M_Z^2}{M_Z^2} = 0.01 \pm 0.12$$

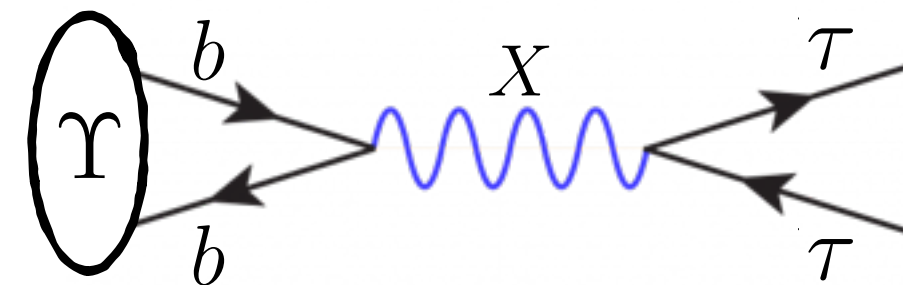
## $\Upsilon$ to $\tau\tau$

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$$R_{\tau\mu} \equiv \frac{\Gamma(\Upsilon(1S) \rightarrow \tau^+\tau^-)}{\Gamma(\Upsilon(1S) \rightarrow \mu^+\mu^-)}$$

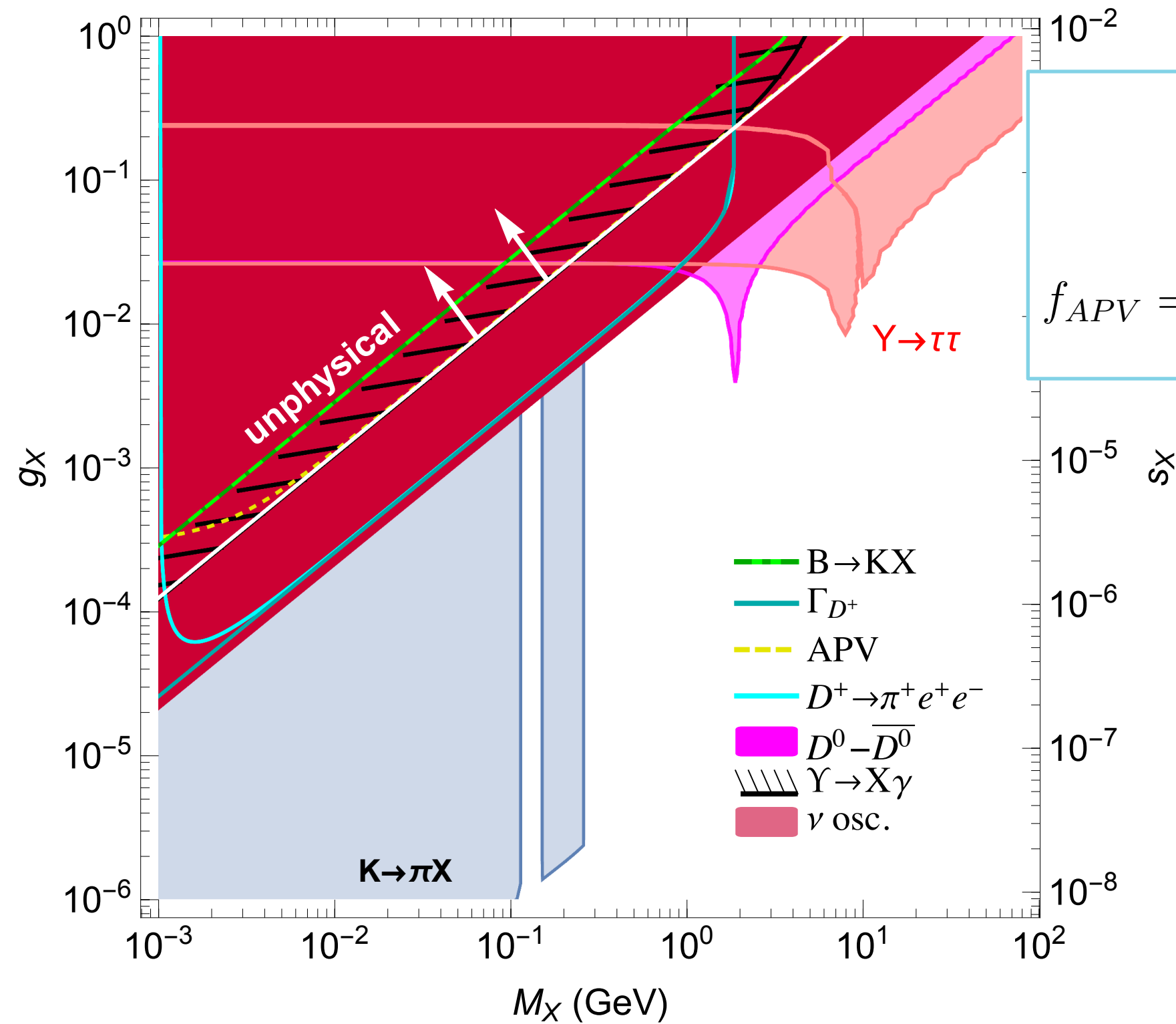
$$1.005 \pm 0.013(\text{stat.}) \pm 0.022(\text{syst.})$$

$$R_{\tau\mu} \simeq 1 - 2 \frac{g_X^2}{e^2} \frac{M_\Upsilon^2}{M_\Upsilon^2 - M_X^2}$$



# Atomic Parity Violation mixing with Z boson

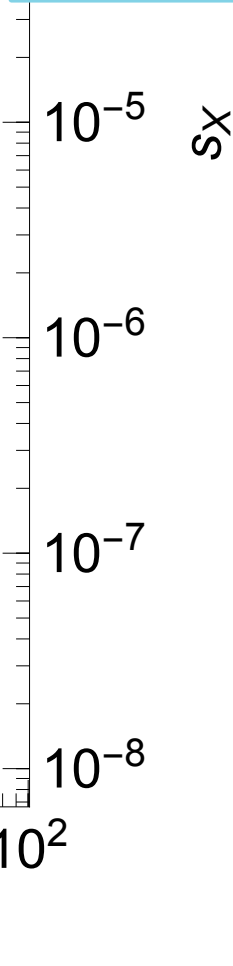
$$\tan\beta = v_2/v_1 = 10$$



$^{133}\text{Cs}$  weak charge

$$Q_W^{SM} = -73.16 \pm 0.3$$

$$f_{APV} = 1 + s_X^2 \frac{M_Z^2}{M_X^2 + q^2} = 1 \pm 0.0063$$





## Scalar sector

$$V = m_{11}^2(\phi_1^\dagger\phi_1) + m_{22}^2(\phi_2^\dagger\phi_2) + m_s^2 s^* s + \frac{\lambda_1}{2}(\phi_1^\dagger\phi_1)^2 + \frac{\lambda_2}{2}(\phi_2^\dagger\phi_2)^2 + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) \quad (24)$$

$$+ \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) + \frac{\lambda_s}{2}(s^* s)^2 + \lambda_{1s}(\phi_1^\dagger\phi_1)(s^* s) + \lambda_{2s}(\phi_2^\dagger\phi_2)(s^* s) - \left[ \mu(\phi_2^\dagger\phi_1)s + \text{h.c.} \right].$$

$$m_A^2 = \mu \frac{v_1^2 v_2^2 + v_1^2 v_s^2 + v_2^2 v_s^2}{\sqrt{2} v_1 v_2 v_s} \quad m_{H^\pm}^2 = \frac{1}{2} \lambda_4 v^2 + \mu \frac{v_s v^2}{\sqrt{2} v_1 v_2}$$

$$y_{ij}'^u \frac{H^\dagger H}{\Lambda^2} \bar{Q}_{iL} \tilde{H} u_{jR} + y_{ij}'^d \frac{H^\dagger H}{\Lambda^2} \bar{Q}_{iL} H d_{jR},$$

$$y'^{u,d} = y_t \begin{pmatrix} c_\beta m_u / m_t & 0 & -s_\beta V_{ub} \\ 0 & c_\beta m_c / m_t & -s_\beta V_{cb} \\ 0 & 0 & c_\beta \end{pmatrix}$$

# Z to f f X

Light X (longitudinal enhancement):

$$\Gamma(Z \rightarrow f \bar{f} X) = \frac{N_c}{192\pi^3} M_Z |y_f^{GX}|^2 \left[ g_V^f{}^2 \left( 1 + \log \frac{M_Z^2}{M_X^2} \right) + g_A^f{}^2 \left( -\frac{14}{3} + \log \frac{M_Z^2}{M_X^2} \right) \right]$$

Heavy X (transverse modes):

$$\frac{d\Gamma(Z \rightarrow f \bar{f} X)}{dx} = \frac{M_Z}{6\pi^3} \left[ (g_V^f c_V^f + g_A^f c_A^f)^2 (h_1(x) + h_3(x)) \right]$$

$$h_1(x) = 2x \log \frac{x + \sqrt{x^2 - 4R}}{x - \sqrt{x^2 - 4R}} + \sqrt{x^2 - 4R} \left( \frac{1}{R} + R - x - \frac{x}{R} + \frac{x^2}{12R} - \frac{7}{3} \right)$$

$$h_3(x) = \frac{4(1+R-x)(1+R)}{x} \log \frac{x + \sqrt{x^2 - 4R}}{x - \sqrt{x^2 - 4R}} - \sqrt{x^2 - 4R} \left( \frac{1}{R} + R - x - \frac{x}{R} + \frac{x^2}{12R} + \frac{5}{3} \right)$$

Marciano Wyler 1979

$$c_V^f \equiv (c_{fR} + c_{fL}), \quad c_A^f \equiv (c_{fR} - c_{fL})$$

$$g_V^\tau = \frac{g}{4c_w} (4s_w^2 - 1), \quad g_A^\tau = \frac{g}{4c_w}, \quad g_V^b = \frac{g}{4c_w} \left( \frac{4s_w^2}{3} - 1 \right), \quad g_A^b = \frac{g}{4c_w}$$

# Meson oscillation

$$(\Delta m_S)_X = \frac{\sqrt{2}}{6} G_F f_S^2 m_S B_S \eta_S \frac{M_Z^2}{m_S^2 - M_X^2} \left| \frac{2g_X^2 U_{ij}^X / 3}{g/c_w} \right|^2$$

$$K - \bar{K} : \left( \frac{100 \text{ GeV}}{m_\varphi} \right) \text{Re} \left( \frac{h_{21}^d}{\sqrt{2} m_s / v} \right) \lesssim 1.4 \times 10^{-2}$$

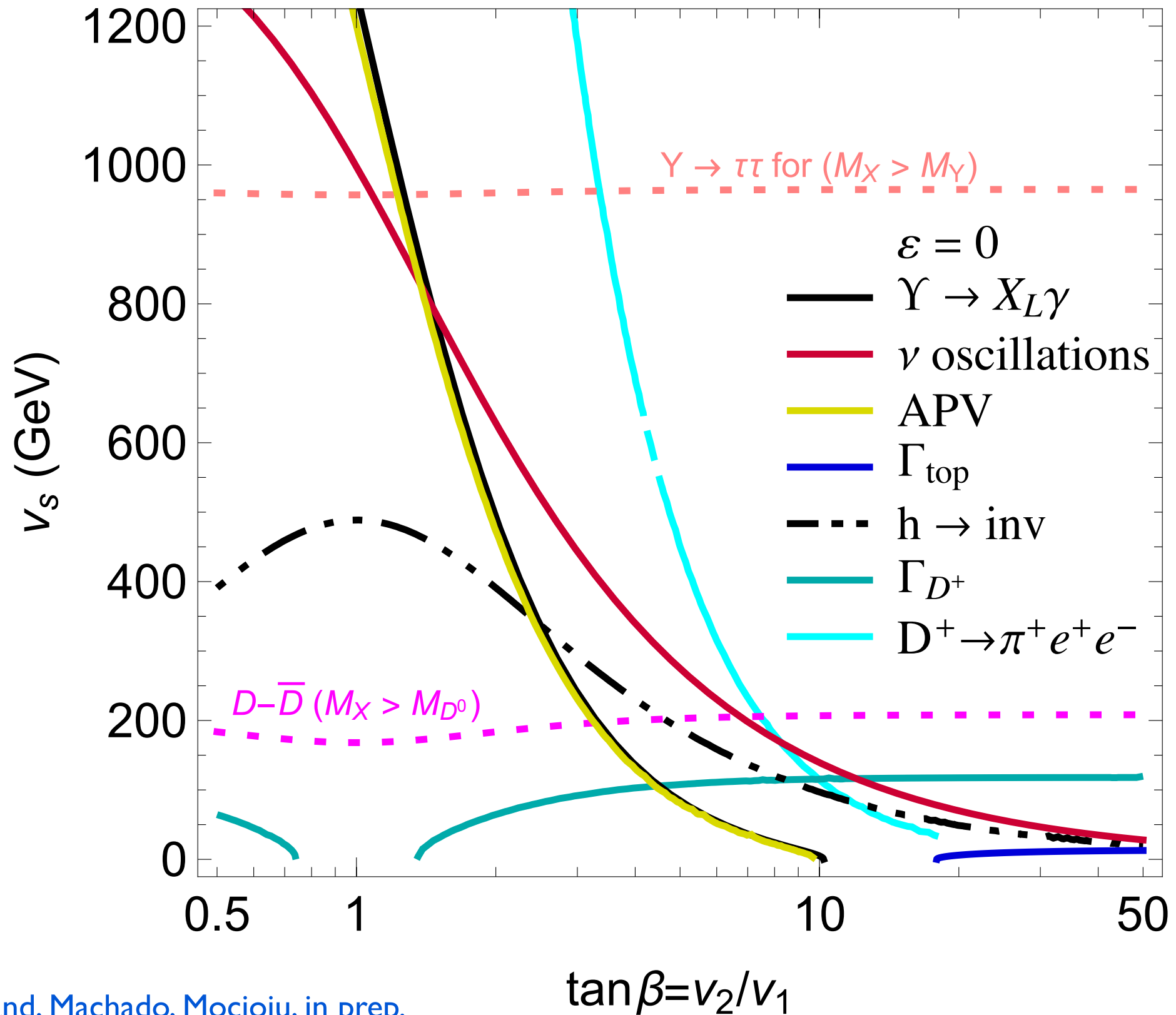
$$B_d - \bar{B}_d : \left( \frac{100 \text{ GeV}}{m_\varphi} \right) \text{Re} \left( \frac{h_{31}^d}{\sqrt{2} m_b / v} \right) \lesssim 3.1 \times 10^{-3}$$

$$B_s - \bar{B}_s : \left( \frac{100 \text{ GeV}}{m_\varphi} \right) \text{Re} \left( \frac{h_{32}^d}{\sqrt{2} m_b / v} \right) \lesssim 1.3 \times 10^{-2}$$

$$D - \bar{D} : \left( \frac{100 \text{ GeV}}{m_\varphi} \right) \text{Re} \left( \frac{h_{12}^u}{\sqrt{2} m_c / v} \right) \lesssim 3.4 \times 10^{-3}$$

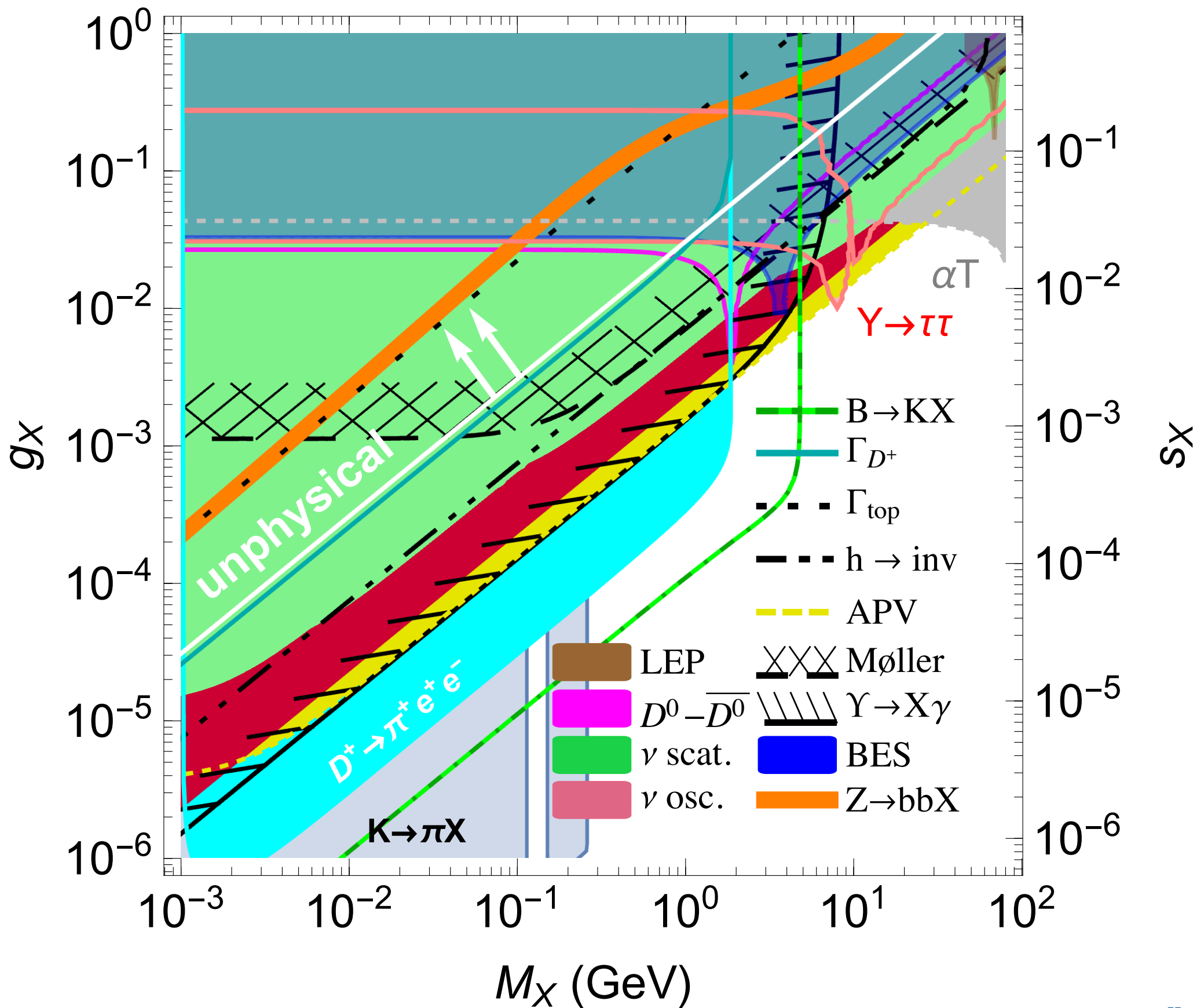
Babu Meng 2009  
Babu Nandi 2000  
Nir Silverman 1990  
Buras Jamin Weisz 1990  
Lenz 2012

# Phenomenology

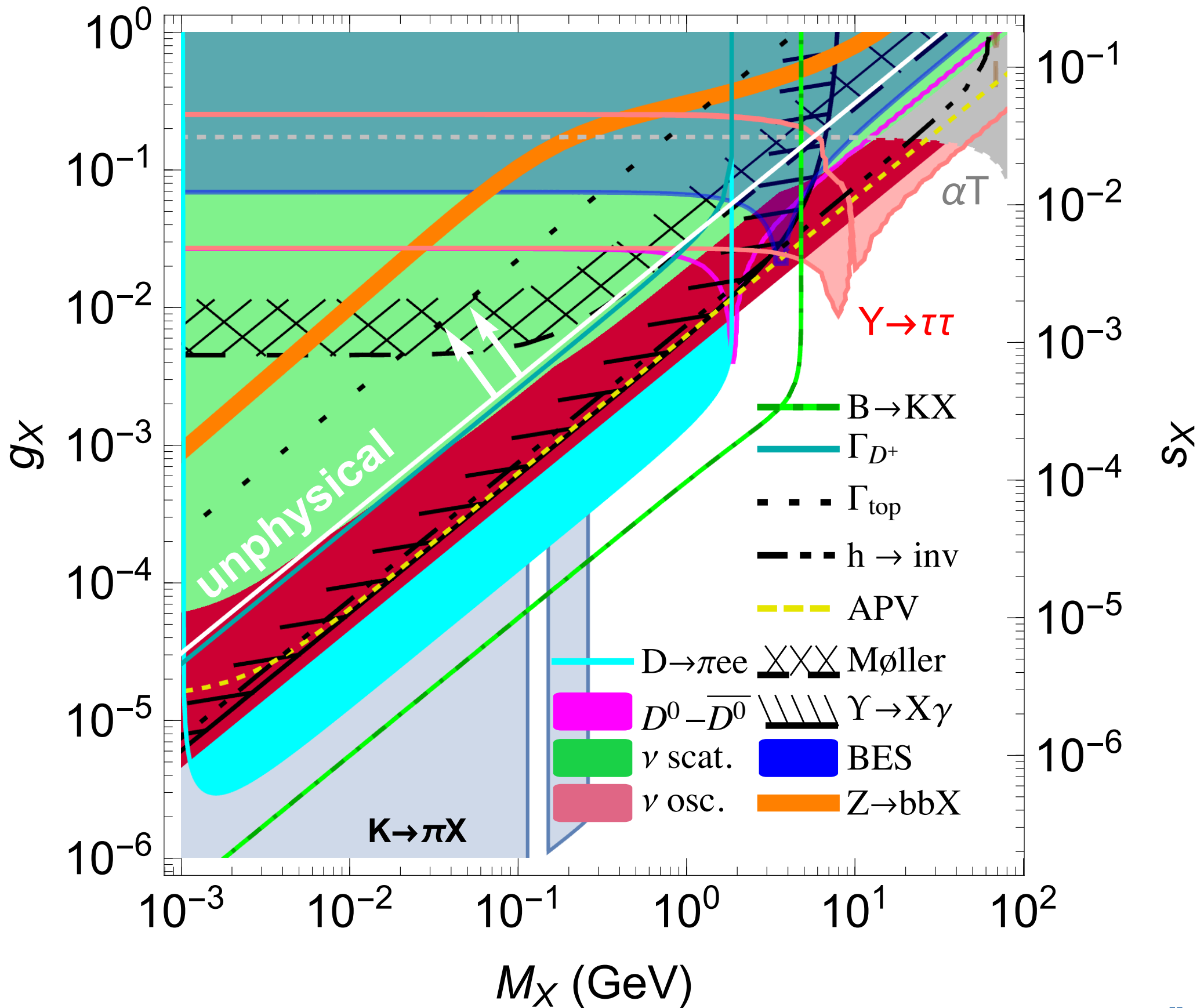


Babu, Friedland, Machado, Mocioiu, in prep.

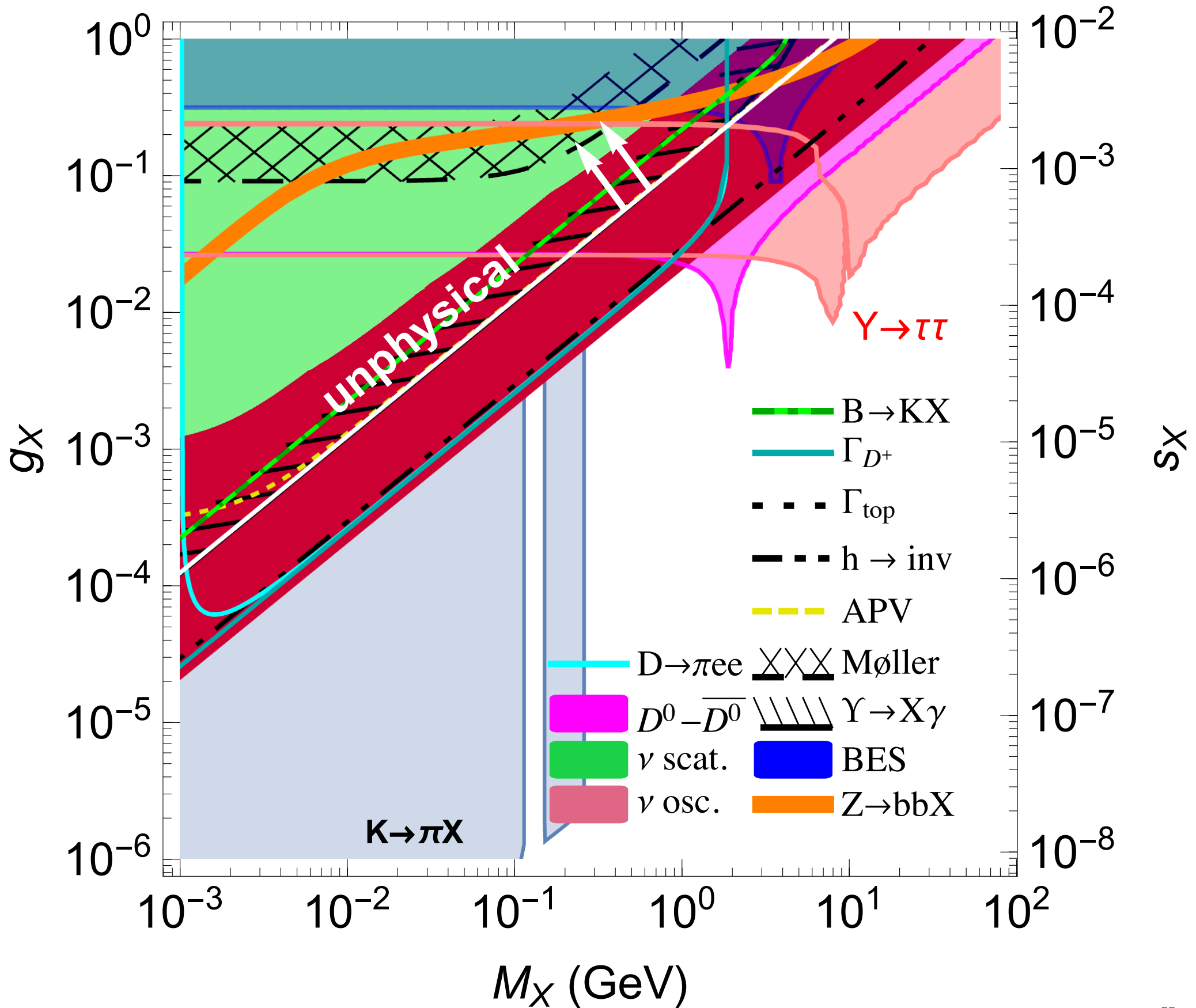
$$\tan\beta = v_2/v_1 = 0.5$$



$$\tan\beta = v_2/v_1 = 2$$



$$\tan\beta = v_2/v_1 = 10$$



$$\tan\beta = v_2/v_1 = 25$$

